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Development of Fuel Cell System Simulator

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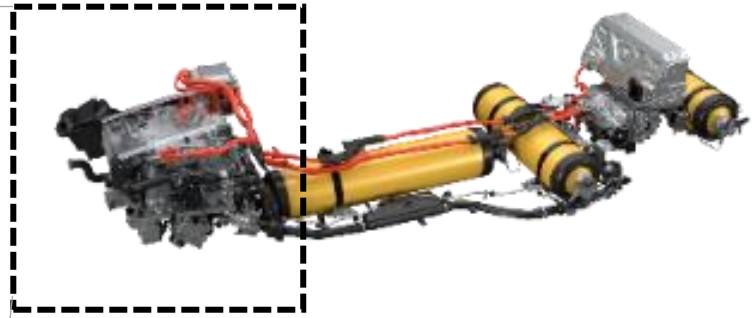
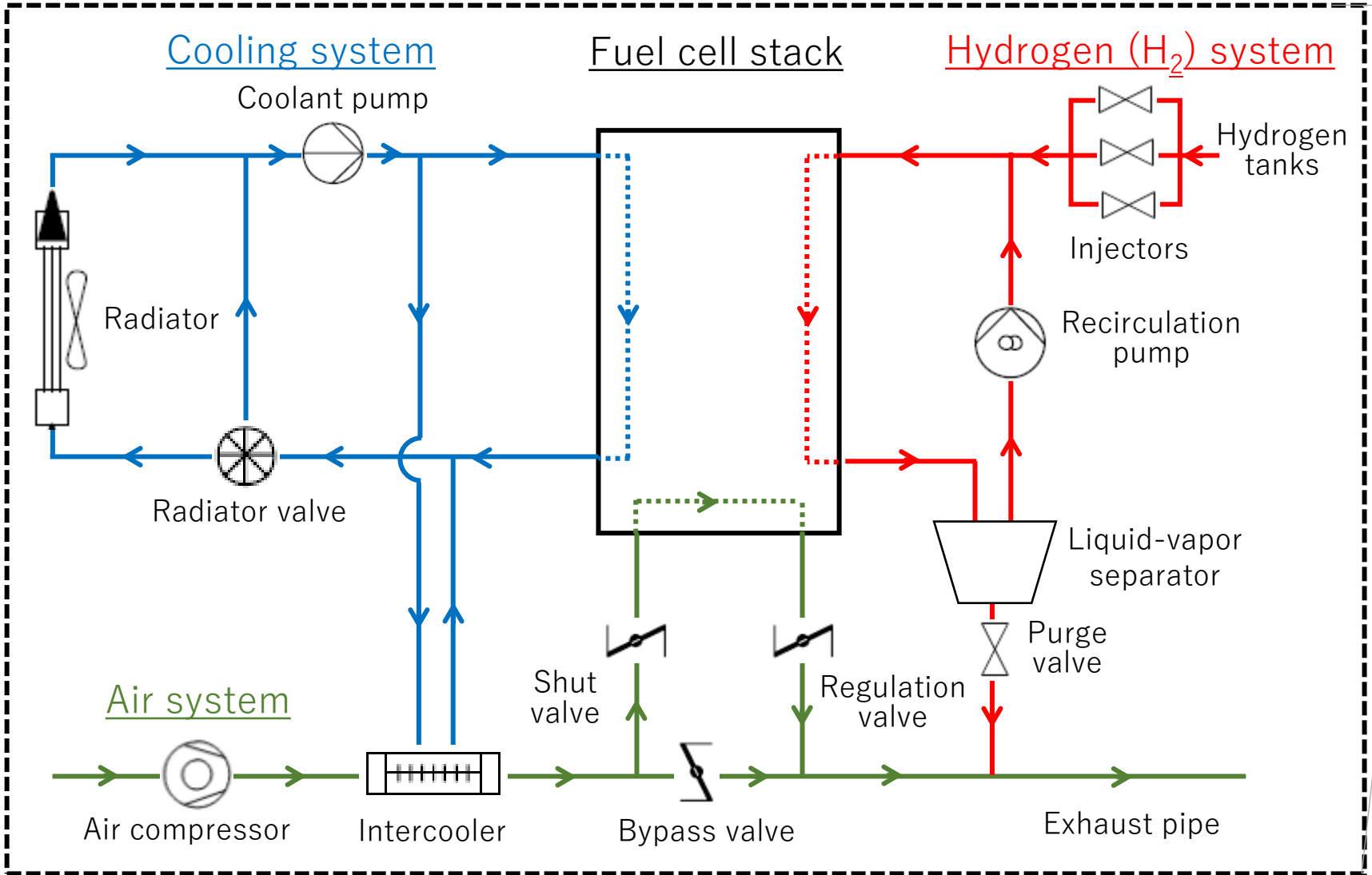
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Outline

1. Background
 - Overview of fuel cell (FC) system
 - Challenges in FC system development process
2. Integrated fuel cell system simulator 
3. Modeling methods of FC system
 - FC system component models
 - Numerical methods
 - Efficient Implementation methods to MATLAB[®] / Simulink[®]
 - Parameter determination
4. Model validation & verification by database collected with state-of-the-art commercial FCEV, 2nd-generation MIRAI
5. Simulation results of overall FC system dynamics

1. Background : Overview of fuel cell (FC) system

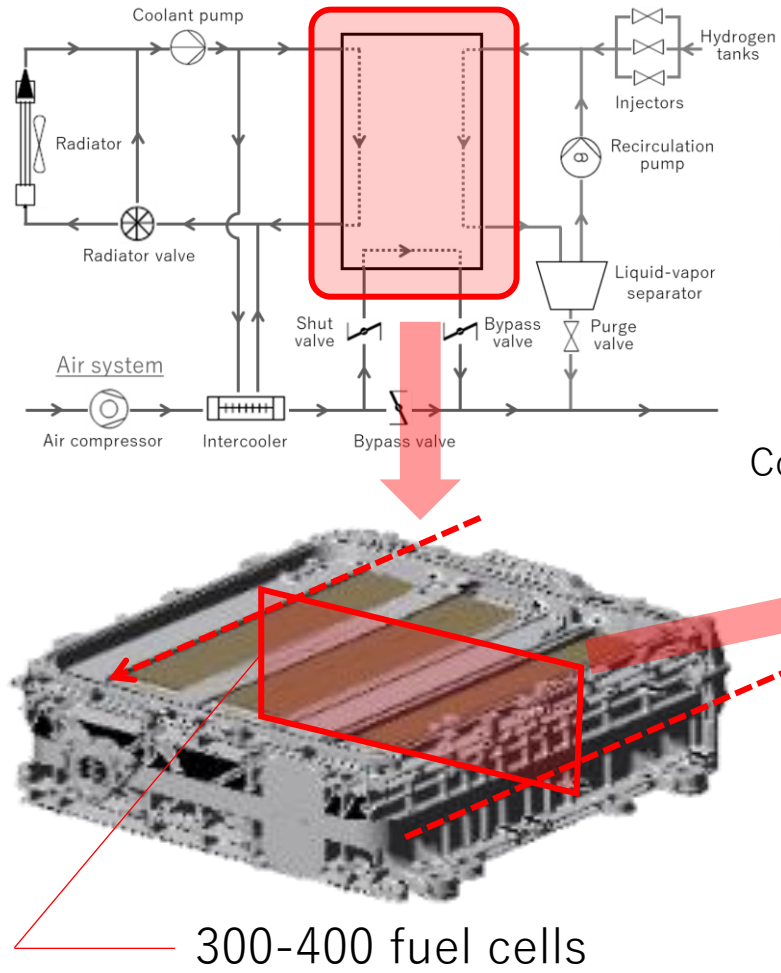


	ICE-system	FC-system
Main engine	Internal combustion engine	FC-stack
sub-systems	Air intake system	Air system
	Fuel injection system	H ₂ system
	Cooling system	Cooling system

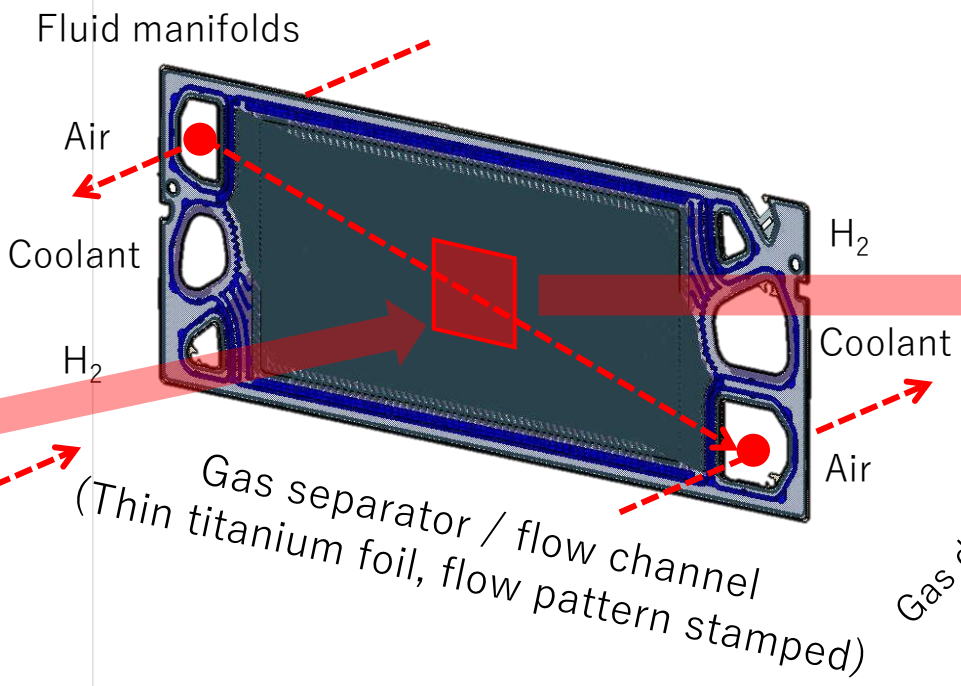
FC-stack as main engine and 3 subsystems of air, H₂, and cooling system
 Similar configuration as internal combustion engine system

1. Background : Fuel cell stack

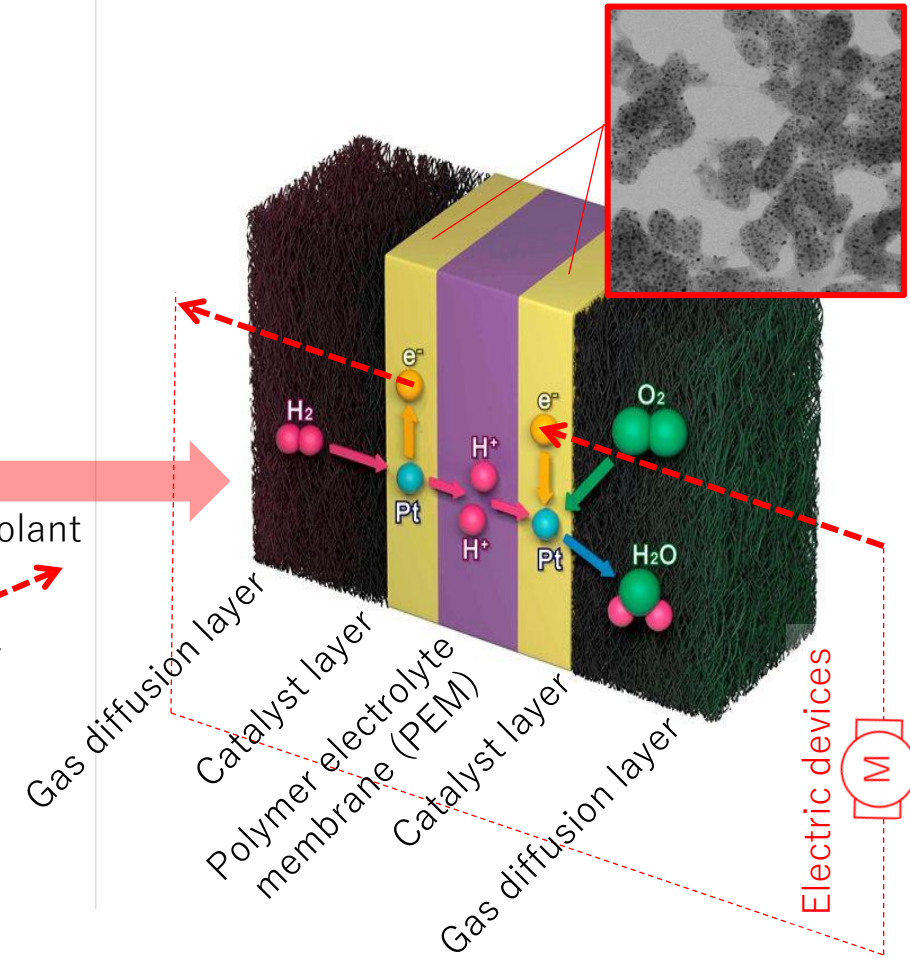
Fuel cell (FC) stack



Fuel cell
(7-layer sandwich structure)



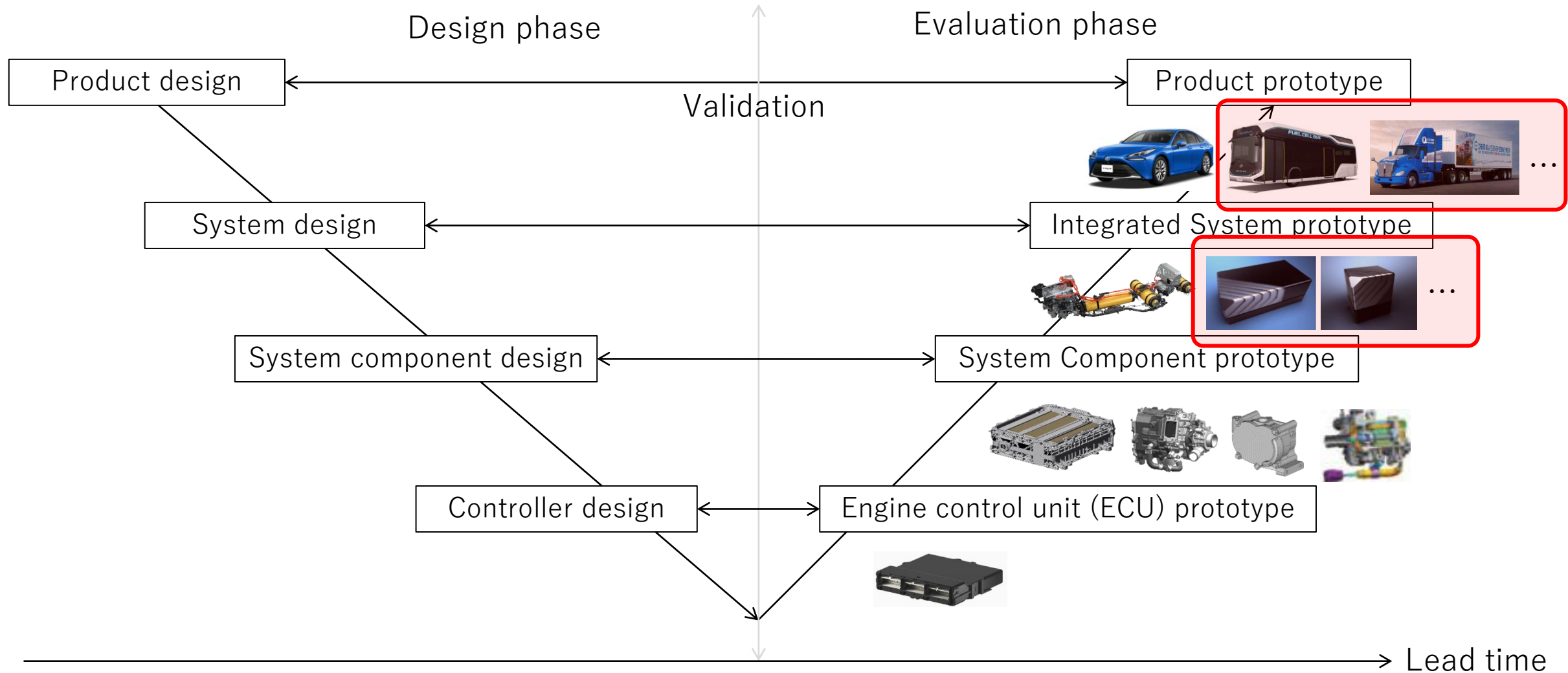
Power generation element
(MEA = Membrane Electrode Assembly)



300-400 fuel cells

Reactants (H₂ and O₂) are supplied to the catalyst layers through the flow channels
Generated electric power is delivered to the external electric devices

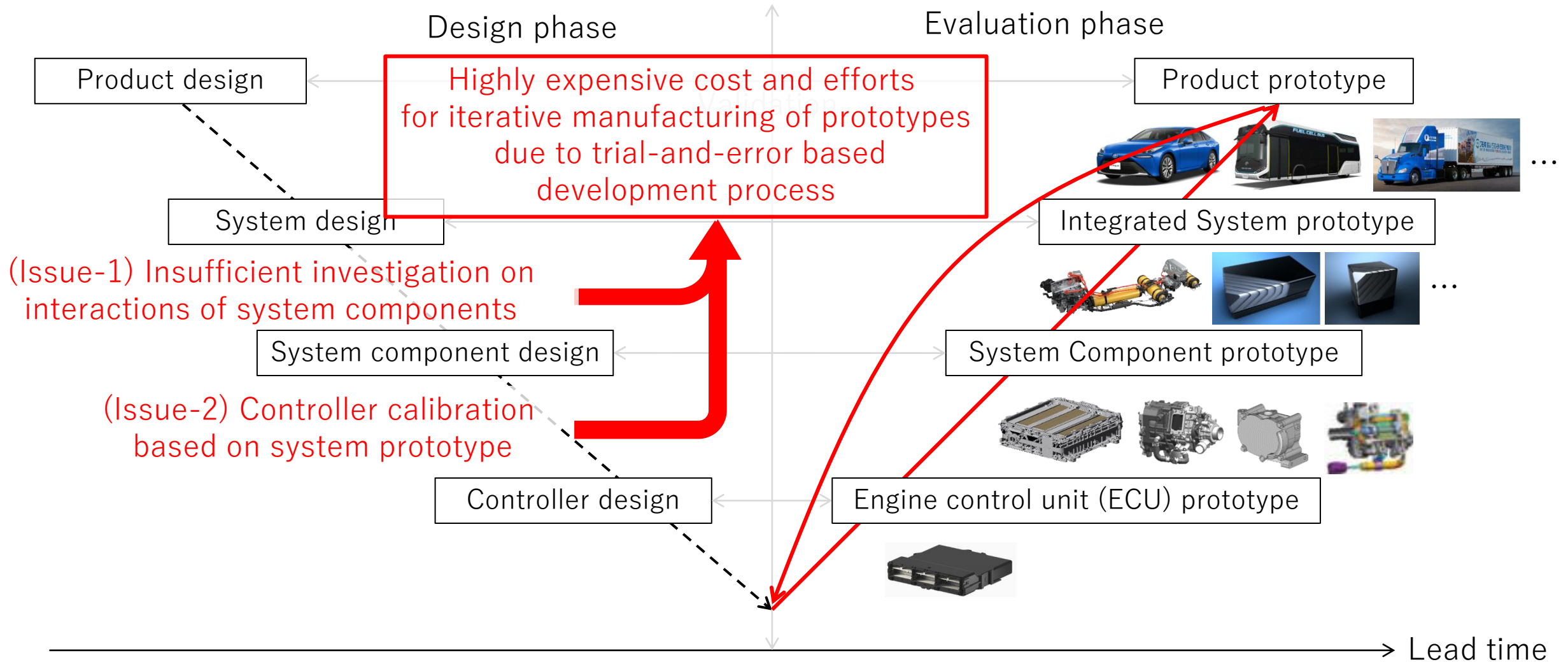
1. Background : Issues in FC system development process



Challenge

- Application of FC system to the various purpose for enhancement of H₂ utilization
- Development of multiple products in parallel with limited development resources

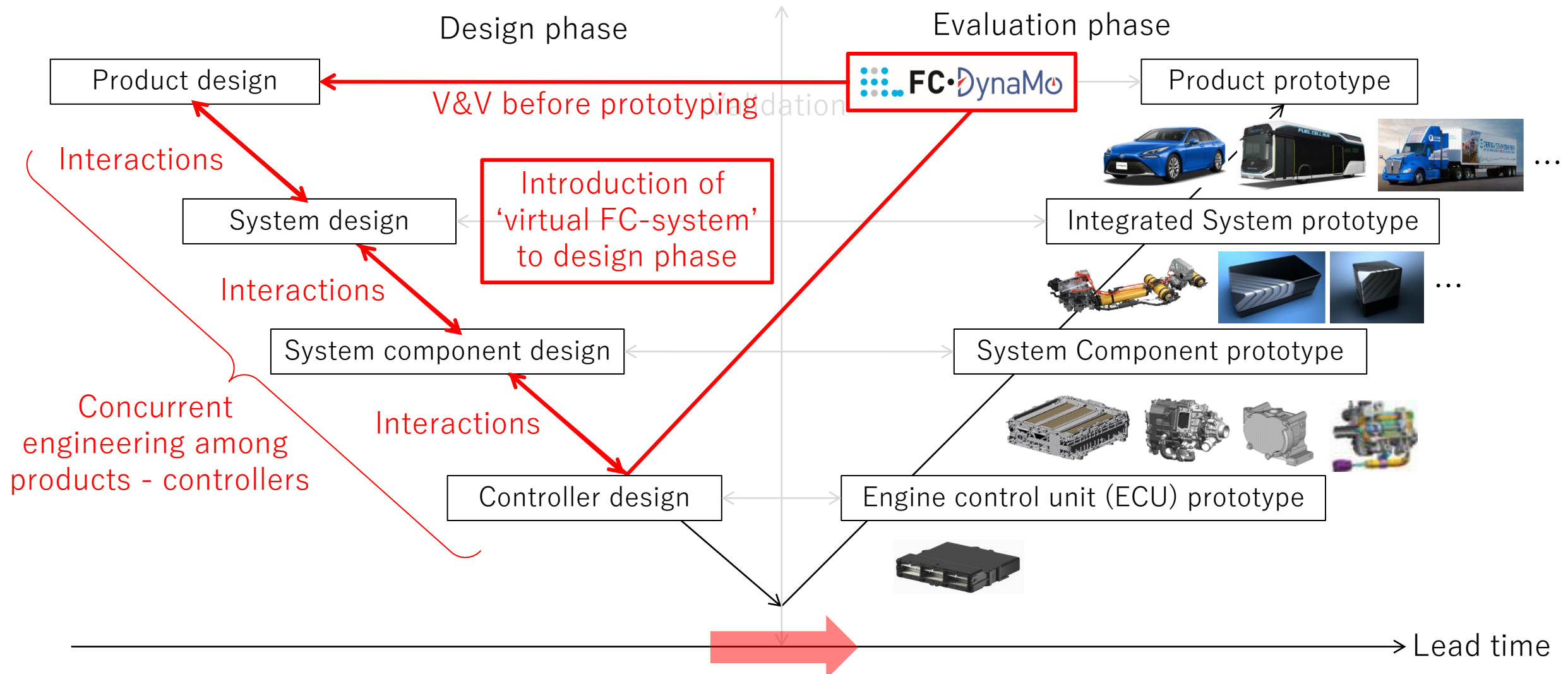
1. Background : Issues in FC system development process



Issue

Highly expensive cost and effort required to trial-and-error based development process
 → One of the largest barriers to enter the fuel cell industry and enhancement of H₂ industry

1. Background : Issues in FC system development process

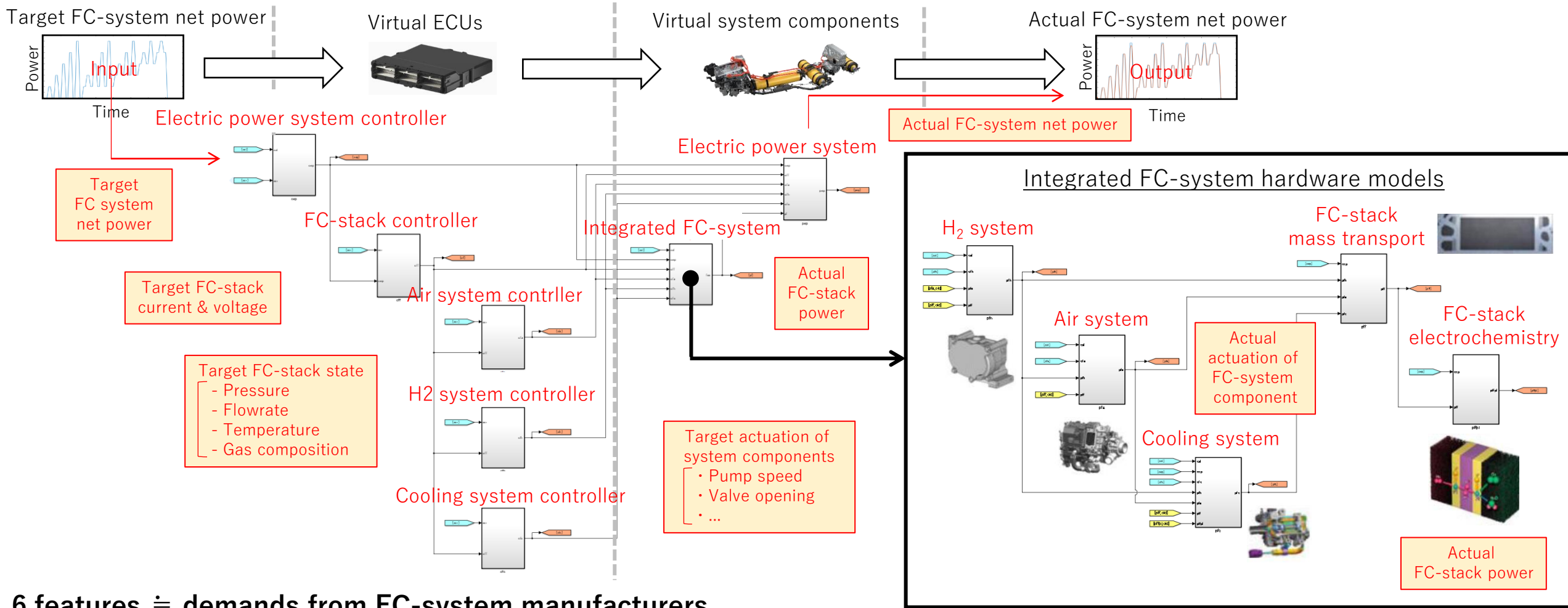


Solution

Prototypes with prospective goal achievement

Concurrent engineering of product, system, component, and controller design considering interaction of components and controllers by introducing 'virtual FC system' in design phase

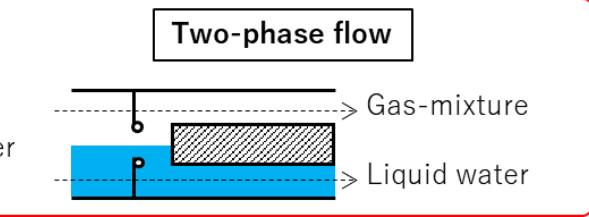
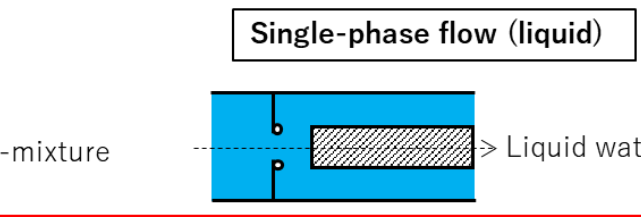
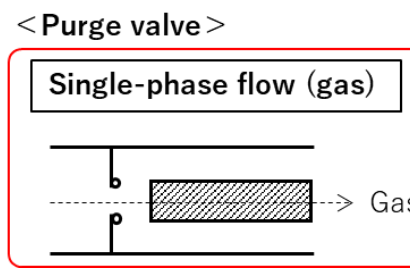
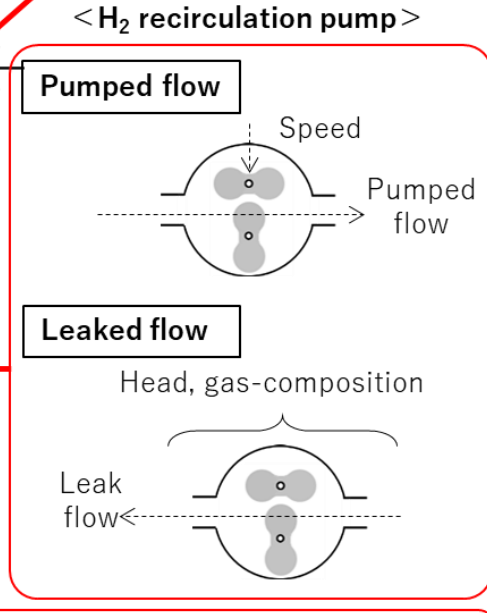
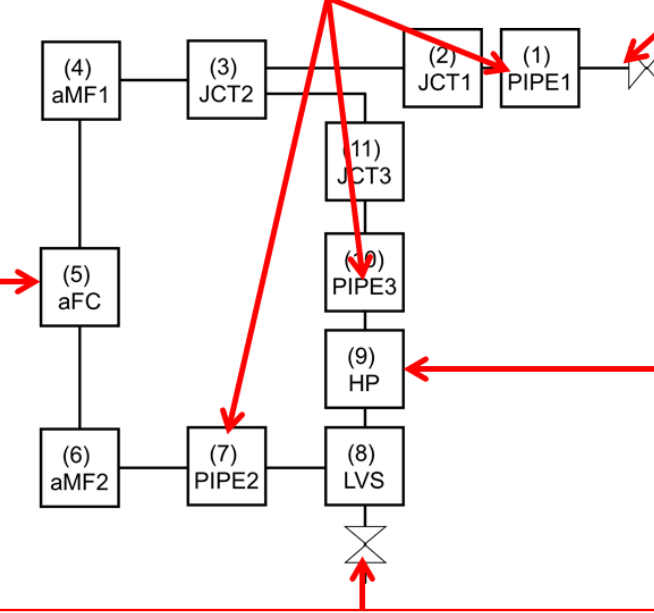
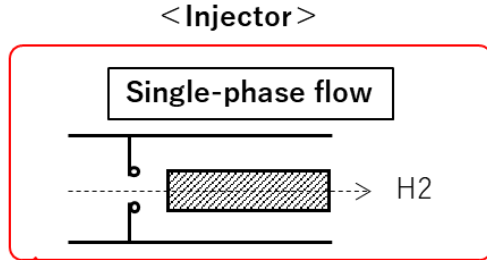
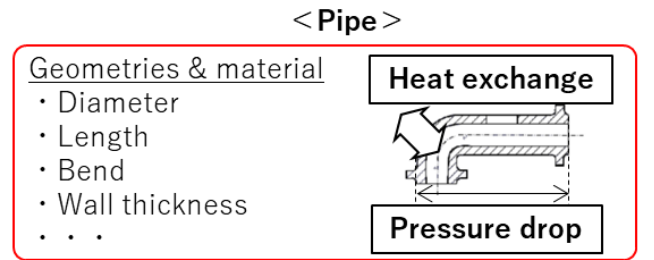
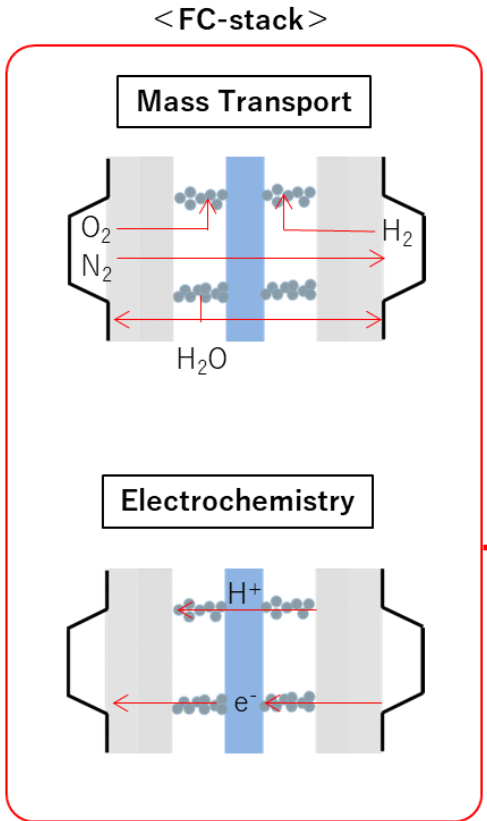
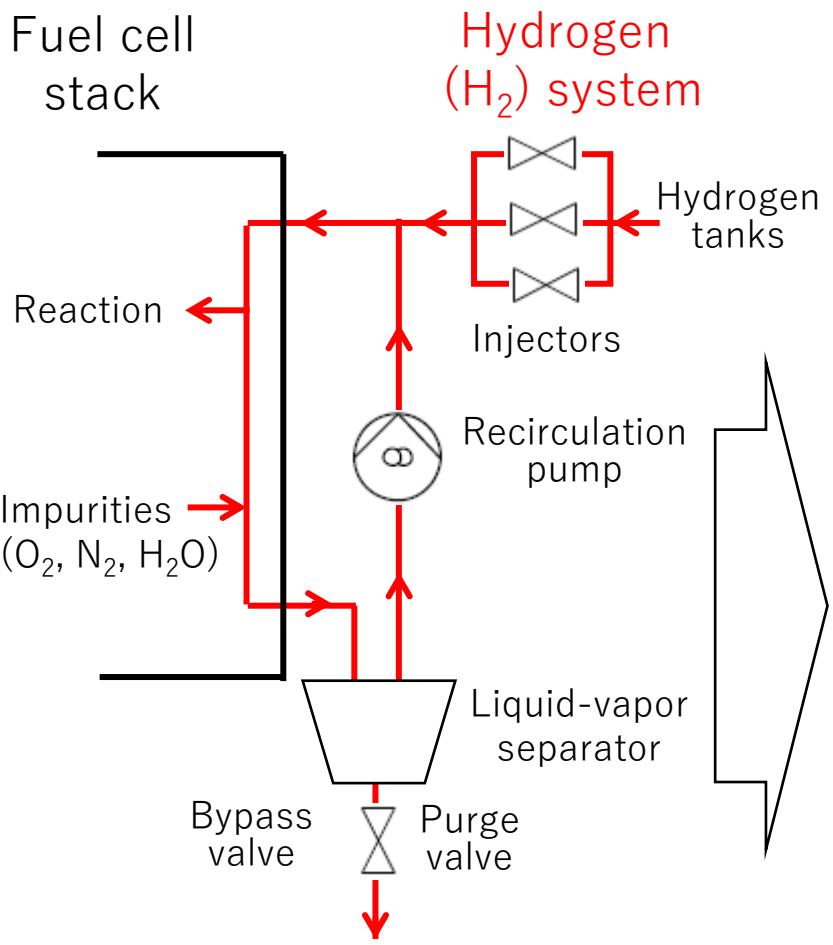
2. Integrated FC-system simulator



6 features \doteq demands from FC-system manufacturers

- **Comprehensiveness** : Physical models in system hardware & controllers in the entire system are included
- **Multi-scale** : Physics of m-scale system component & nm-scale FC-stack materials are included
- **Dynamics** : Dynamic system behaviors of an entire FC-system can be simulated
- **Computational speed** : x50 acceleration than the real time for the benefit of a year-long durability simulation purpose
- **Accuracy** : Validation and verification by the database collected with a commercial FCEV (Gen.2 MIRAI).
- **Usability/Customizability** : Implemented on MATLAB[®]/ Simulink[®] without additional toolboxes, all the codes are white-box

3. Physical modeling of FC-system : Modeling strategy

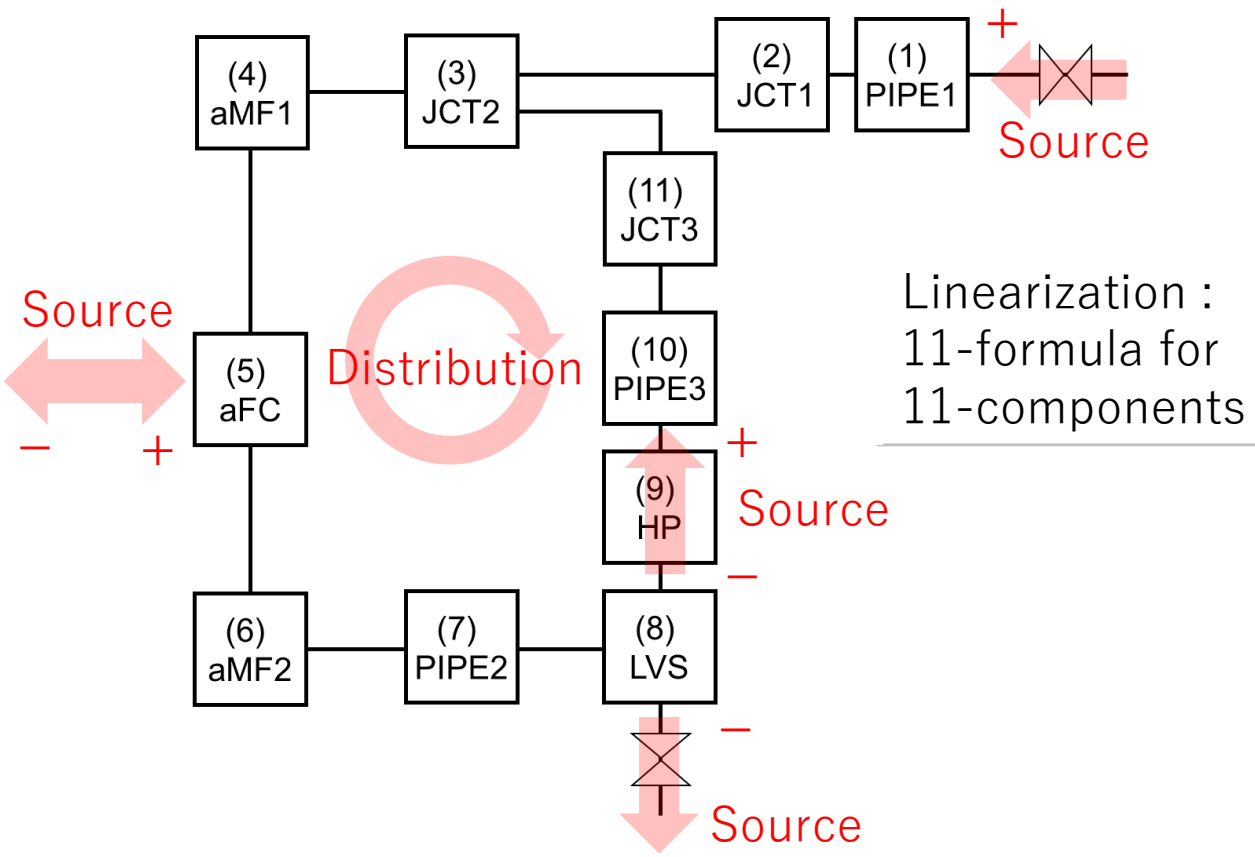


Function-block diagram

- Entire system is broken-down into component level, and expressed as connection of function-blocks
- State variables of pressure, flowrate, temperature, and gas composition across the system
- 1D physical models of mass-transport, electrochemistry in FC-stack and dynamics in system

3. Physical modeling of FC system : Numerical methods

Function block diagram



Mass balance
(Pressure)

molar balance
(Concentration of
O₂, H₂, N₂, and H₂O)

Energy balance
(Temperature)

Algebraic equations

$$\begin{matrix}
 (1) \text{ PIPE1} \\
 (2) \text{ JCT1} \\
 (3) \text{ JCT2} \\
 (4) \text{ aMF1} \\
 (5) \text{ aFC} \\
 (6) \text{ aFC2} \\
 (7) \text{ PIPE2} \\
 (8) \text{ LVS} \\
 (9) \text{ HP} \\
 (10) \text{ PIPE3} \\
 (11) \text{ JCT3}
 \end{matrix}
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 p_{tot}^{(1)} \\
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 \end{pmatrix}$$

$$\begin{matrix}
 (1) \text{ PIPE1} \\
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 (8) \text{ LVS} \\
 (9) \text{ HP} \\
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 (11) \text{ JCT3}
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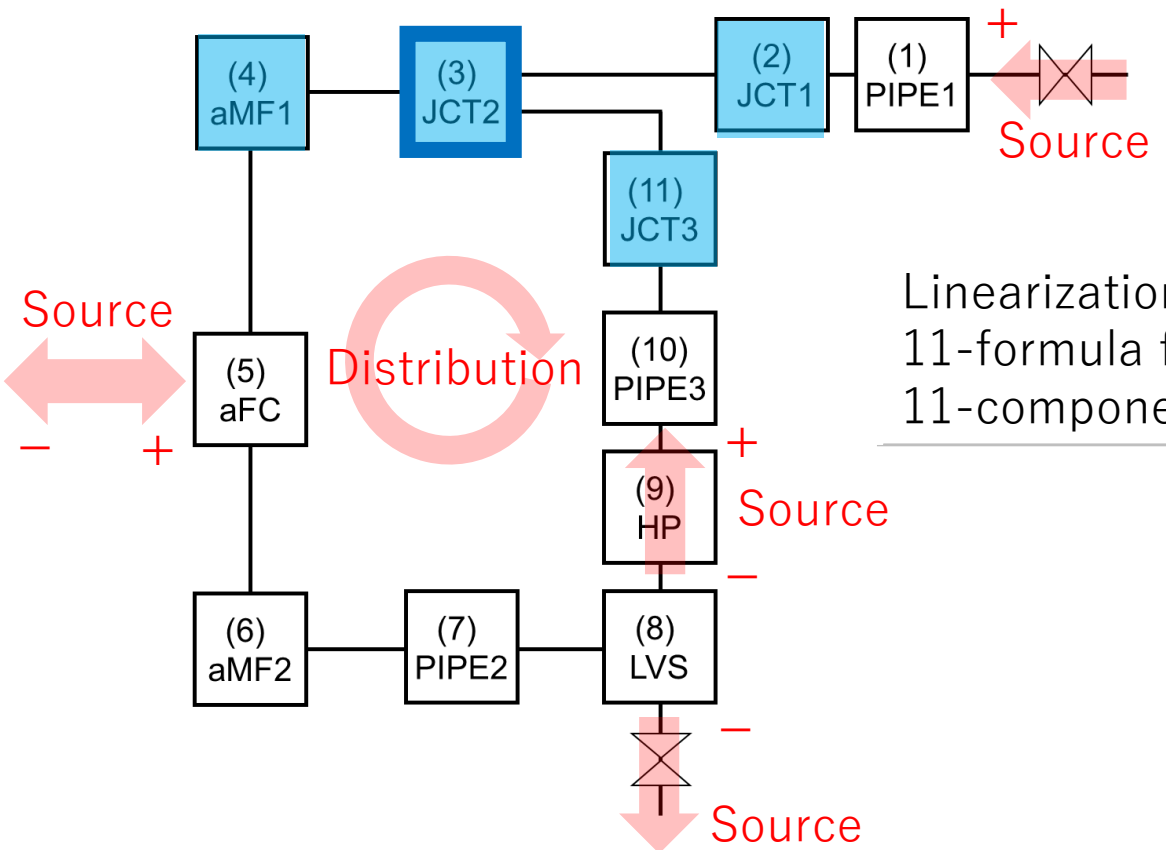
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 \end{matrix}
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 b^{(7)} \\
 b^{(8)} \\
 b^{(9)} \\
 b^{(10)} \\
 b^{(11)}
 \end{pmatrix}$$

Features

- Algebraic equations to describe mass balance, molar balance, and energy balance in system
- ‘How the source term affects the distribution in one time step ?’ is expressed in each equation
- In-house and white-box numerical solvers for future improvement and customization

3. Physical modeling of FC system : Numerical methods

Function block diagram



Linearization :
11-formula for
11-components

Mass balance
(Pressure)

molar balance
(Concentration of
O₂, H₂, N₂, and H₂O)

Energy balance
(Temperature)

Algebraic equations

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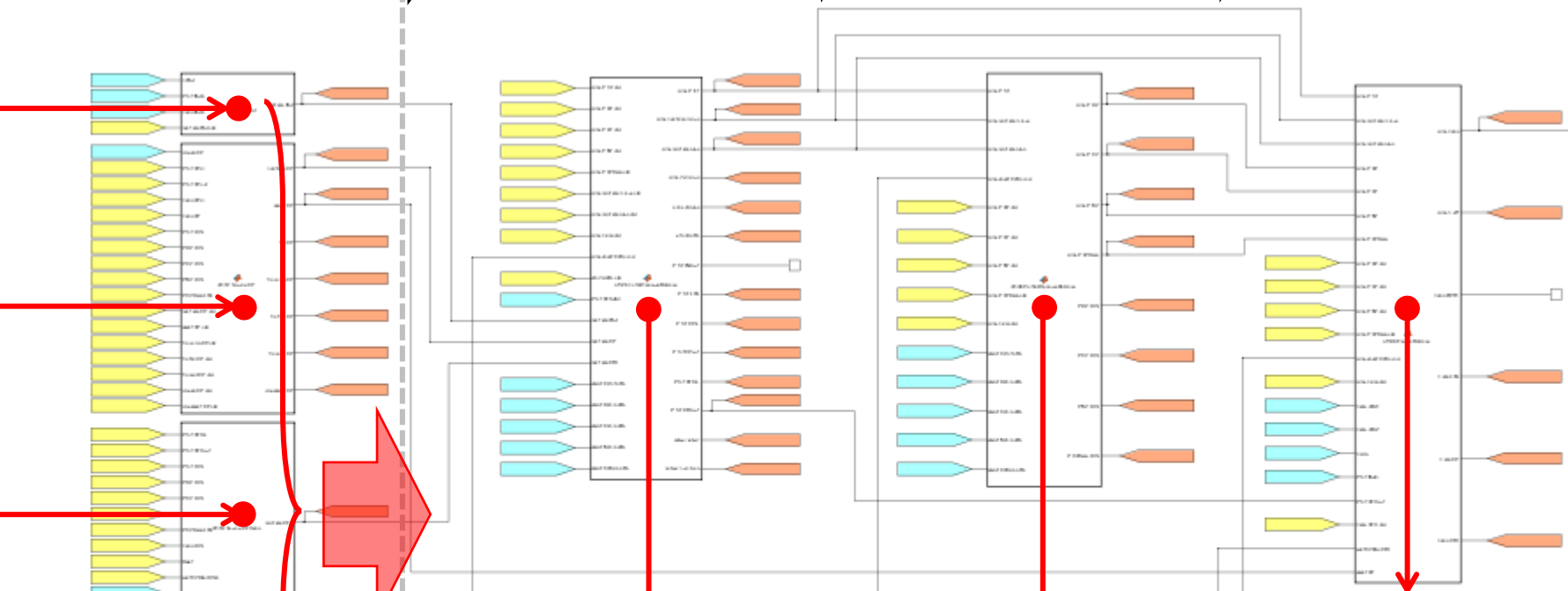
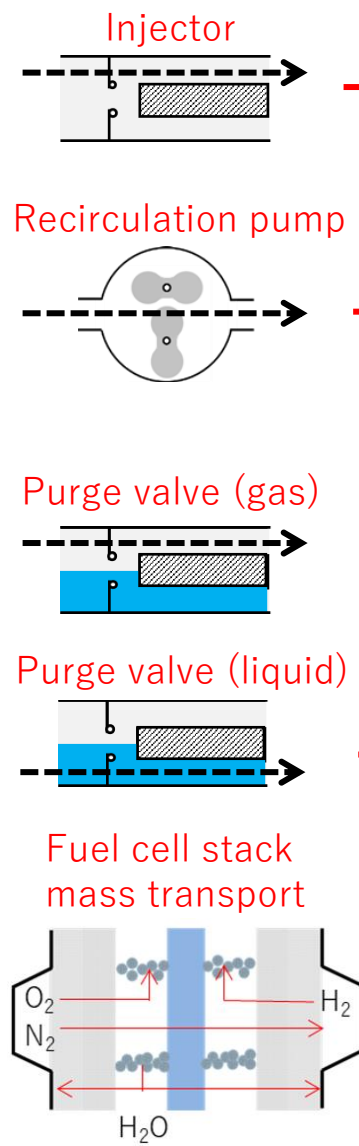
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$$\begin{matrix}
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 (2) \text{ JCT1} \\
 (3) \text{ JCT2} \\
 (4) \text{ aMF1} \\
 (5) \text{ aFC} \\
 (6) \text{ aFC2} \\
 (7) \text{ PIPE2} \\
 (8) \text{ LVS} \\
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 \end{matrix}
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 \end{pmatrix}^{-1}
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 b^{(1)} \\
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 T^{aFC1} \\
 b^{(7)} \\
 b^{(8)} \\
 b^{(9)} \\
 b^{(10)} \\
 b^{(11)}
 \end{pmatrix}$$

Features

- Algebraic equations to describe mass balance, molar balance, and energy balance in system
- ‘How the source term affects the distribution in one time step ?’ is expressed in each equation
- In-house and white-box numerical solvers for future improvement and customization

3. Physical modeling of FC system : Implementation to MATLAB/Simulink



From external functions

Mass balance

$$\begin{pmatrix} (1) \\ (2) \\ (3) \text{ JCT2} \\ (4) \text{ aMF1} \\ (5) \text{ aFC} \\ (6) \text{ aFC2} \\ (7) \text{ PIPE2} \\ (8) \text{ LVS} \\ (9) \text{ HP} \\ (10) \text{ PIPE3} \\ (11) \text{ JCT3} \end{pmatrix} \begin{pmatrix} F_{tot}^{(3)} \\ F_{tot}^{(4)} \\ F_{tot}^{(5)} \\ F_{tot}^{(6)} \\ F_{tot}^{(7)} \\ F_{tot}^{(8)} \\ F_{tot}^{(9)} \\ F_{tot}^{(10)} \\ F_{tot}^{(11)} \end{pmatrix} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & a^{(3)(2)} & a^{(3)(3)} & a^{(3)(4)} & 0 & 0 & 0 & 0 & 0 & 0 & a^{(3)(11)} \\ 0 & 0 & a^{(4)(3)} & a^{(4)(4)} & a^{(4)(5)} & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & a^{(5)(4)} & a^{(5)(5)} & a^{(5)(6)} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & a^{(6)(5)} & a^{(6)(6)} & a^{(6)(7)} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & a^{(7)(6)} & a^{(7)(7)} & a^{(7)(8)} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & a^{(8)(7)} & a^{(8)(7)} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & a^{(9)(9)} & a^{(9)(10)} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & a^{(10)(9)} & a^{(10)(10)} & a^{(10)(11)} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & a^{(11)(10)} & a^{(11)(11)} \end{pmatrix}^{-1} \begin{pmatrix} b^{(1)} \\ b^{(2)} \\ b^{(3)} \\ b^{(4)} \\ b^{(5)} \\ b^{(6)} \\ b^{(7)} \\ b^{(8)} \\ b^{(9)} \\ b^{(10)} \\ b^{(11)} \end{pmatrix}$$

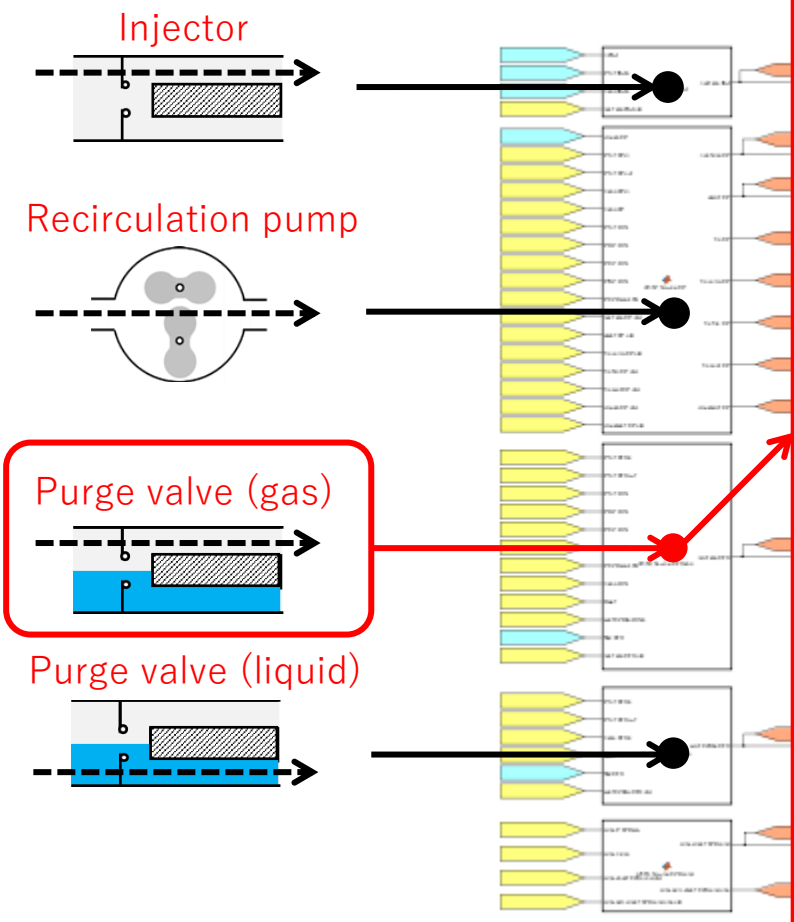
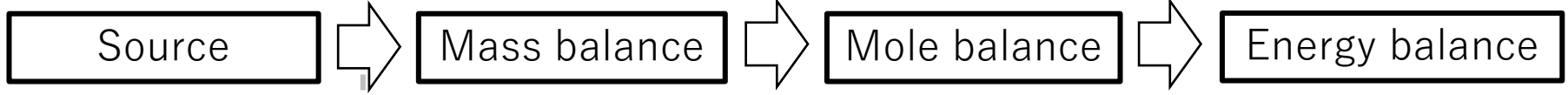
Molar balance

$$\begin{pmatrix} (1) \\ (2) \end{pmatrix} \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}^{-1} \begin{pmatrix} b^{(1)} \\ b^{(2)} \\ b^{(3)} \\ b^{(4)} \\ b^{(5)} \\ b^{(6)} \\ b^{(7)} \\ b^{(8)} \\ b^{(9)} \\ b^{(10)} \\ b^{(11)} \end{pmatrix}$$

Energy balance

$$\begin{pmatrix} (1) \\ (2) \end{pmatrix} \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}^{-1} \begin{pmatrix} b^{(1)} \\ b^{(2)} \\ b^{(3)} \\ b^{(4)} \\ b^{(5)} \\ b^{(6)} \\ b^{(7)} \\ b^{(8)} \\ b^{(9)} \\ b^{(10)} \\ b^{(11)} \end{pmatrix}$$

3. Physical modeling of FC system : Implementation to MATLAB/Simulink



Spec-book

Implementation

$$\text{if } \frac{P_{tot}^{HEVout}}{P_{tot}^{HEVin}} < \left(\frac{2}{\gamma+1}\right)^{\frac{\gamma}{\gamma-1}} \cong 0.5283, \quad \dot{m}_{gas}^{HEV} = A_{HEV}^{eff} \frac{P_{tot}^{HEVin}}{\sqrt{R_{gas}^{HEVin} T_{gas}^{HEVin}}} \sqrt{\left(\frac{2\gamma}{\gamma-1}\right) \left[\left(\frac{2}{\gamma+1}\right)^{\frac{\gamma}{\gamma-1}} - \left(\frac{2}{\gamma+1}\right)^{\frac{\gamma+1}{\gamma}} \right]}$$

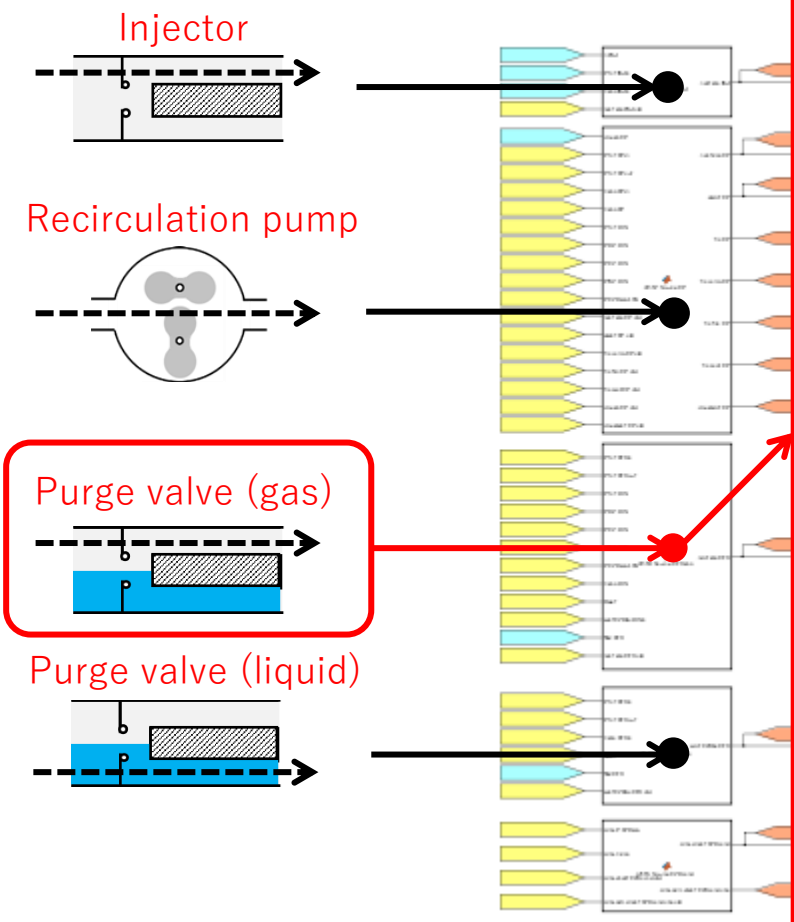
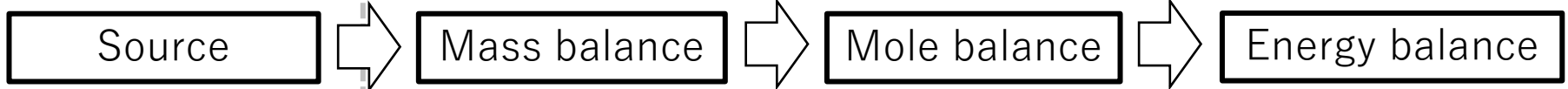
$$\text{else } \dot{m}_{gas}^{HEV} = A_{HEV}^{eff} \frac{P_{tot}^{HEVin}}{\sqrt{R_{gas}^{HEVin} T_{gas}^{HEVin}}} \sqrt{\left(\frac{2\gamma}{\gamma-1}\right) \left[\left(\frac{P_{tot}^{HEVout}}{P_{tot}^{HEVin}}\right)^{\frac{2}{\gamma}} - \left(\frac{P_{tot}^{HEVout}}{P_{tot}^{HEVin}}\right)^{\frac{\gamma+1}{\gamma}} \right]}$$

```

% Choked flow
if P_out/P_in < (2/(gamma_gas+1))^(gamma_gas/(gamma_gas-1))
% Mass-flowrate at HEV [mol/min]
mdot = A_HEV
* eta_HEV_gas1
* eta_HEV_gas2
* (P_in/sqrt(R_gas * T_in))
* sqrt(2*gamma_gas/(gamma_gas-1))
* sqrt(((2/(gamma_gas+1))^(gamma_gas/(gamma_gas-1)))^(2/gamma_gas)
- ((2/(gamma_gas+1))^(gamma_gas/(gamma_gas-1)))^((gamma_gas+1)/gamma_gas));Q
% Subsonic flow
elseif ((2/(gamma_gas+1))^(gamma_gas/(gamma_gas-1)) <= P_out/P_in) && (P_out/P_in < 1)
% Mass-flowrate at HEV [mol/min]
mdot = A_HEV
* eta_HEV_gas1
* eta_HEV_gas2
* (P_in/sqrt(R_gas * T_in))
* sqrt(2*gamma_gas/(gamma_gas-1))
* sqrt((P_out/P_in)^(2/gamma_gas) - (P_out/P_in)^((gamma_gas+1)/gamma_gas));
  
```

‘Hybrid-coding’ = Physics in MATLAB + Interaction among physics in Simulink for the benefit of the effort and lead time of coding and reviewing

3. Physical modeling of FC system : Implementation to MATLAB/Simulink

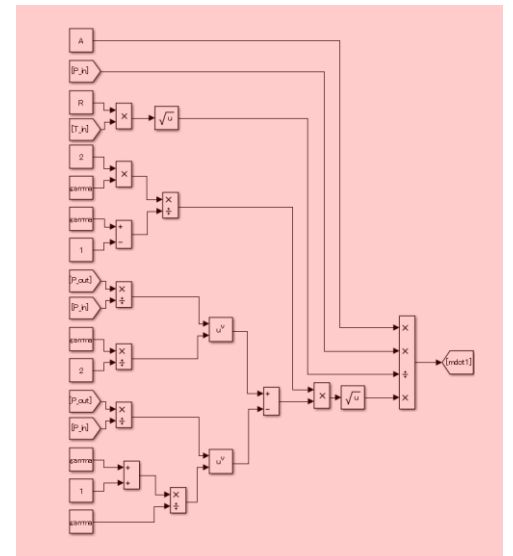
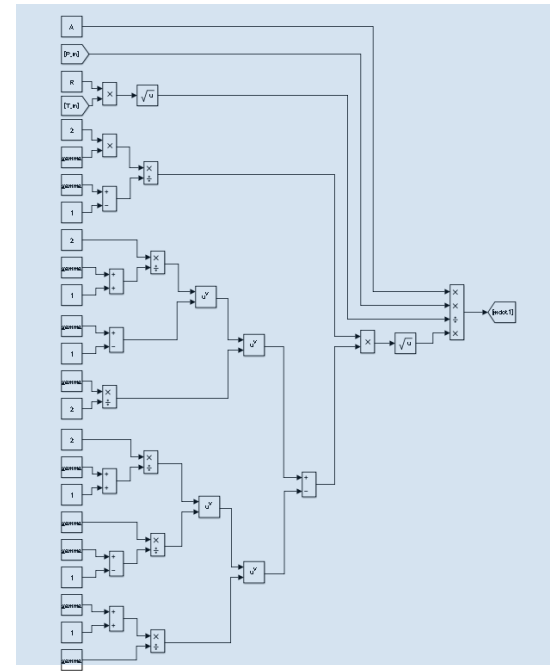
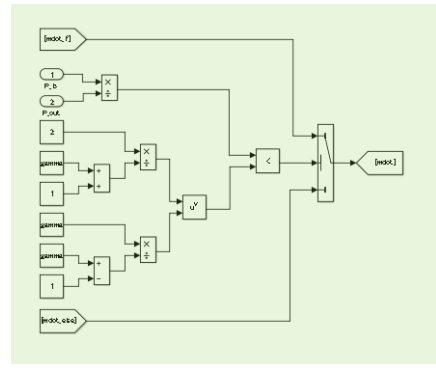


Spec-book

$$\text{if } \frac{p_{tot}^{HEVout}}{p_{tot}^{HEVin}} < \left(\frac{2}{\gamma+1}\right)^{\frac{\gamma}{\gamma-1}} \cong 0.5283, \quad \dot{m}_{gas}^{HEV} = A_{HEV}^{eff} \frac{p_{tot}^{HEVin}}{\sqrt{R_{gas}^{HEVin} T_{gas}^{HEVin}}} \sqrt{\left(\frac{2\gamma}{\gamma-1}\right) \left[\left(\frac{2}{\gamma+1}\right)^{\frac{\gamma}{\gamma-1}} - \left(\frac{2}{\gamma+1}\right)^{\frac{\gamma+1}{\gamma}} \right]}$$

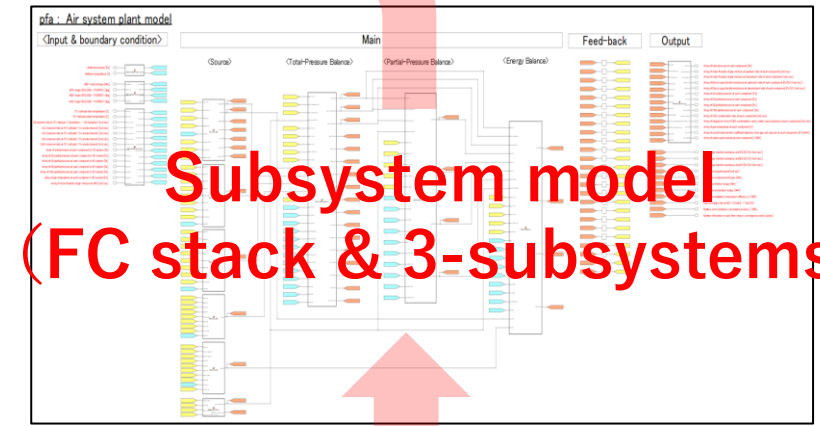
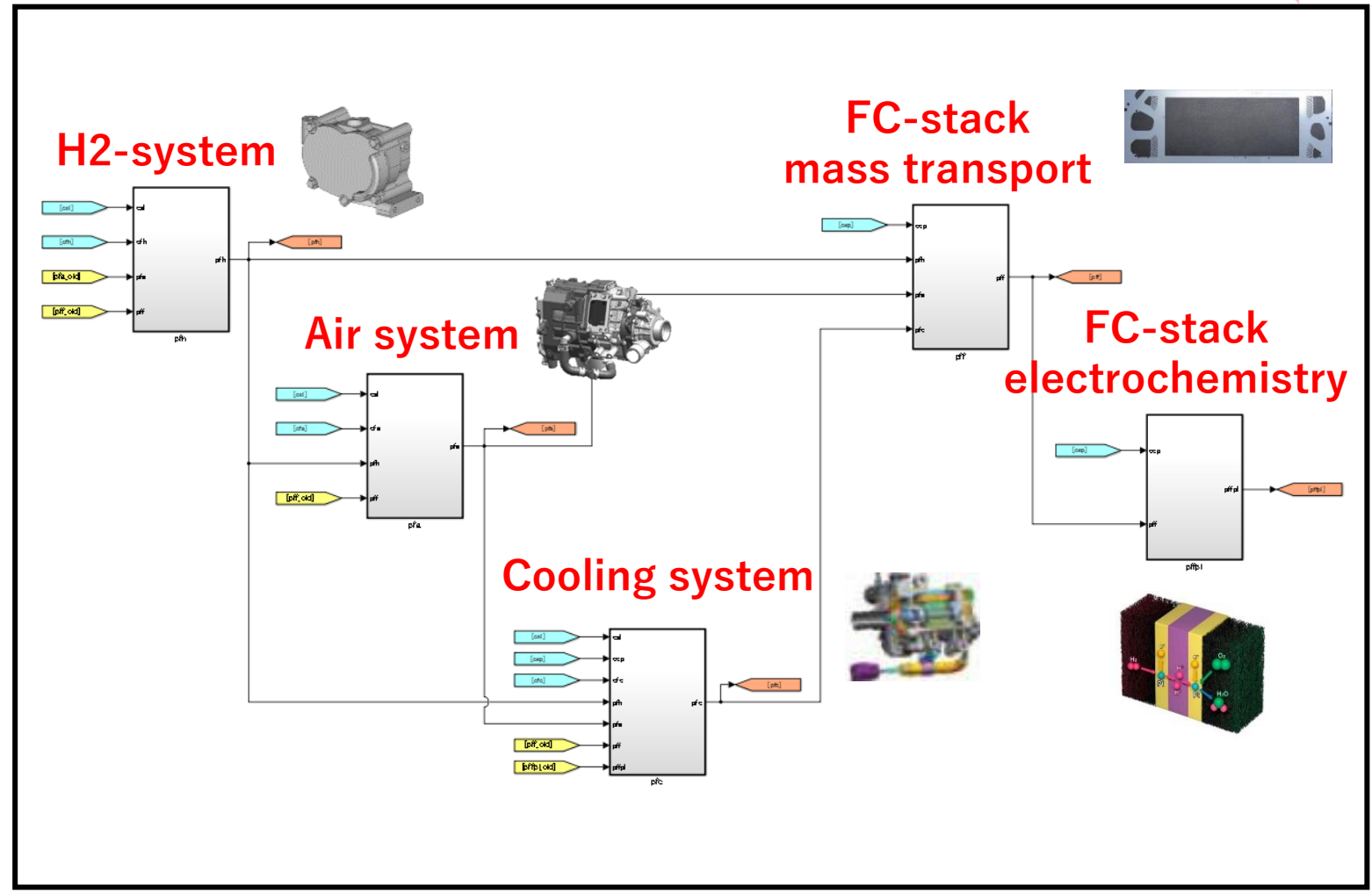
$$\text{else } \dot{m}_{gas}^{HEV} = A_{HEV}^{eff} \frac{p_{tot}^{HEVin}}{\sqrt{R_{gas}^{HEVin} T_{gas}^{HEVin}}} \sqrt{\left(\frac{2\gamma}{\gamma-1}\right) \left[\left(\frac{p_{tot}^{HEVout}}{p_{tot}^{HEVin}}\right)^{\frac{2}{\gamma}} - \left(\frac{p_{tot}^{HEVout}}{p_{tot}^{HEVin}}\right)^{\frac{\gamma+1}{\gamma}} \right]}$$

Implementation (Simulink)



‘Hybrid-coding’ = Physics in MATLAB + Interaction among physics in Simulink for the benefit of the effort and lead time of coding and reviewing

Integrated FC system hardware model



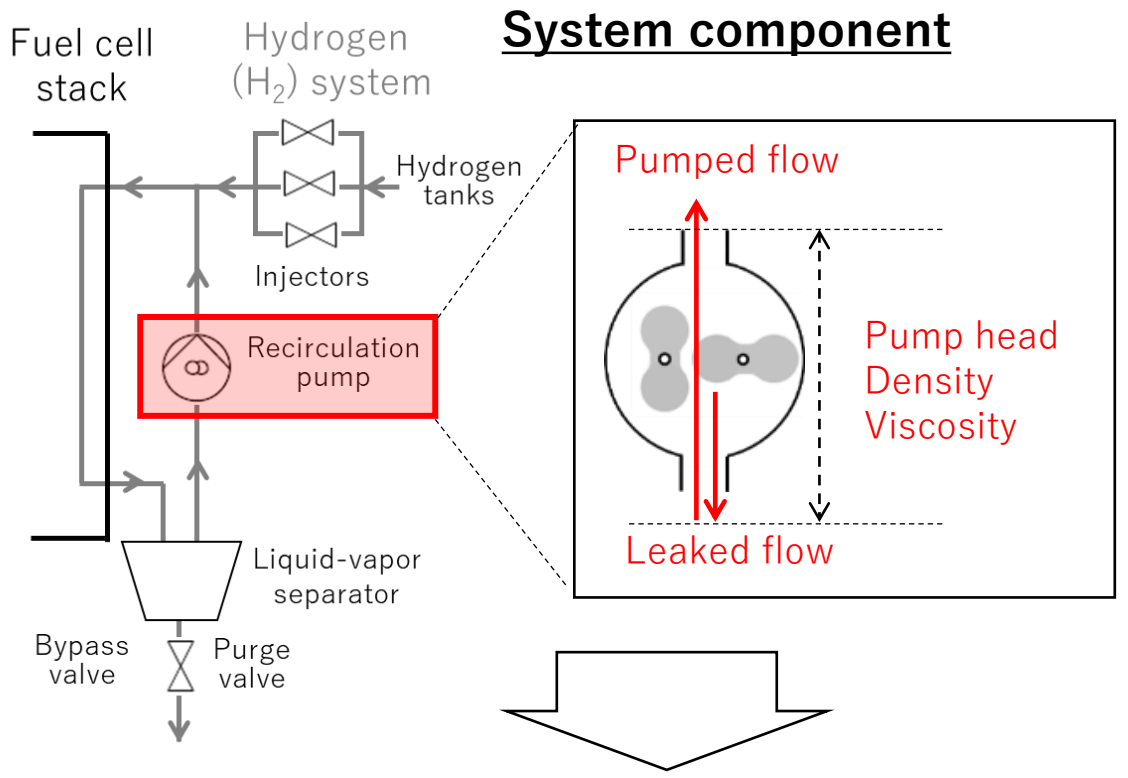
```

function [array_P_tot, array_ndot_gas_minus, array_ndot_gas_plus, array_id_minus, array_id_plus, eta_2d_aFO, P_tot_inOutlet, P_tot_LVS, P_tot_HPIn, P_tot_HPout, P_tot_HEVin, P_tot_HEVout] =
    phys2D_TotalPressureBalance(array_P_tot_old, array_P_02_old, array_P_H2_old, array_P_H2Ovap_old, array_ndot_gas_minus_old, array_ndot_gas_plus_old, array_id_gas_old, array_id_gas_new, P_tot_inlet, ndot_gas_HP, ndot_gas_HEV, dndot_H2cra_aFO, dndot_H2cra_aFO, dndot_H2cra_aFO, dndot_H2Ocond) %Codegen

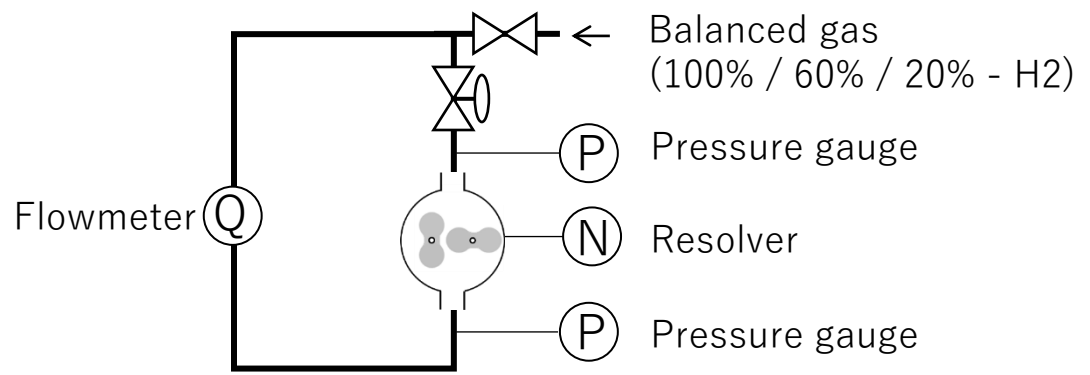
% <function>
% - Calculation of Darcy's gas transfer resistance at each component
% - Calculation of total pressure at each component
% - Calculation of molar flowrate of gas-mixture into/from each component
%
% (Input)
% - array_P_tot_old : Array of total pressure at each component (Old value) [Pa]
% - array_P_02_old : Array of O2 partial pressure at each component (Old value) [Pa]
% - array_P_H2_old : Array of H2 partial pressure at each component (Old value) [Pa]
% - array_P_H2Ovap_old : Array of H2O partial pressure at each component (Old value) [Pa]
% - array_ndot_gas_minus_old : Array of molar flowrate at upper-stream side of each component (Old value) [mol/sec]
% - array_ndot_gas_plus_old : Array of molar flowrate at lower-stream side of each component (Old value) [mol/sec]
% - array_id_gas_old : Array of gas mixture at each component (Old value) [mol/sec]
% - eta_2d_aFO : Darcy's gas transfer resistance at FC anode channel considering liquid-water plugging [1/100k]
% - P_tot_inlet : Total pressure at HP-inlet [Pa]
% - ndot_gas_HP : Molar flowrate of gas-mixture at HP [mol/sec]
% - ndot_gas_HEV : Molar flowrate of gas-mixture at HEV [mol/sec]
% - dndot_H2cra_aFO : Darcy's gas transfer resistance at anode channel [mol/sec]
% - dndot_H2cra_aFO : Darcy's gas transfer resistance at cathode channel [mol/sec]
% - dndot_H2Ocond : H2O condensation rate at each component [mol/sec]
%
% (Output)
% - array_P_tot : Array of total pressure at each component [Pa]
% - array_ndot_gas_minus : Array of molar flowrate at upstream side of each component [mol/sec]
% - array_ndot_gas_plus : Array of molar flowrate at downstream side of each component [mol/sec]
% - array_id_gas : Array of Darcy's gas transfer resistance at downstream side of each component [mol/sec]
% - eta_2d_aFO : Correction ratio of Darcy's gas transfer resistance at FC-cathode channel considering liquid-water plugging [1/100k]
% - P_tot_inOutlet : Total pressure at LVS [Pa]
% - P_tot_LVS : Total pressure at LVS [Pa]
% - P_tot_HPIn : Total pressure at HP-inlet [Pa]
% - P_tot_HPout : Total pressure at HP-outlet [Pa]
% - P_tot_HEVin : Total pressure at HEV-inlet [Pa]
% - P_tot_HEVout : Total pressure at HEV-outlet [Pa]
%
% (Out-functions)
    
```

Individual physical model of FC stack and subsystems are integrated to an entire FC system model

3. Parameters determination : FC system component models



Unit test data (**NOT** system data)

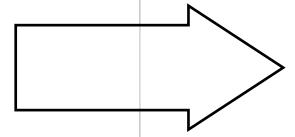


1D system component model

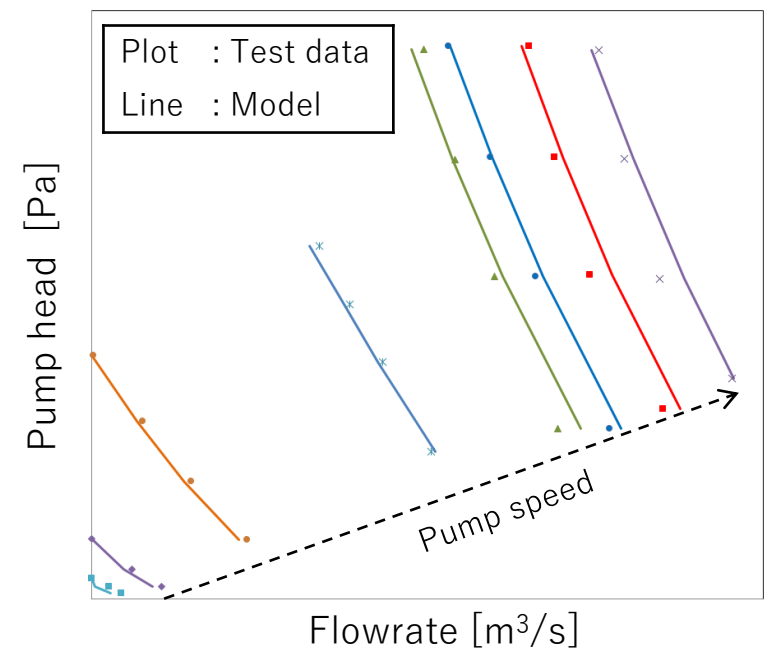
Overall flowrate $\dot{v} = C_1 N - C_2 \frac{\Delta P C_3}{\mu C_4 \rho C_5}$

Pump speed
Pump head

Viscosity
Density



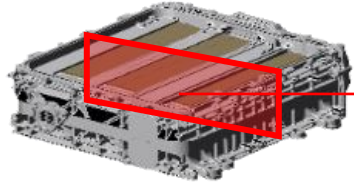
Calibration of $C_1 - C_5$



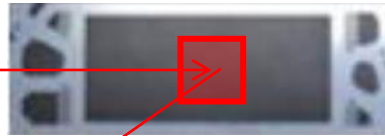
All the parameters can be determined with unit-test data (**NOT** system test data)

3. Parameters determination : FC stack models

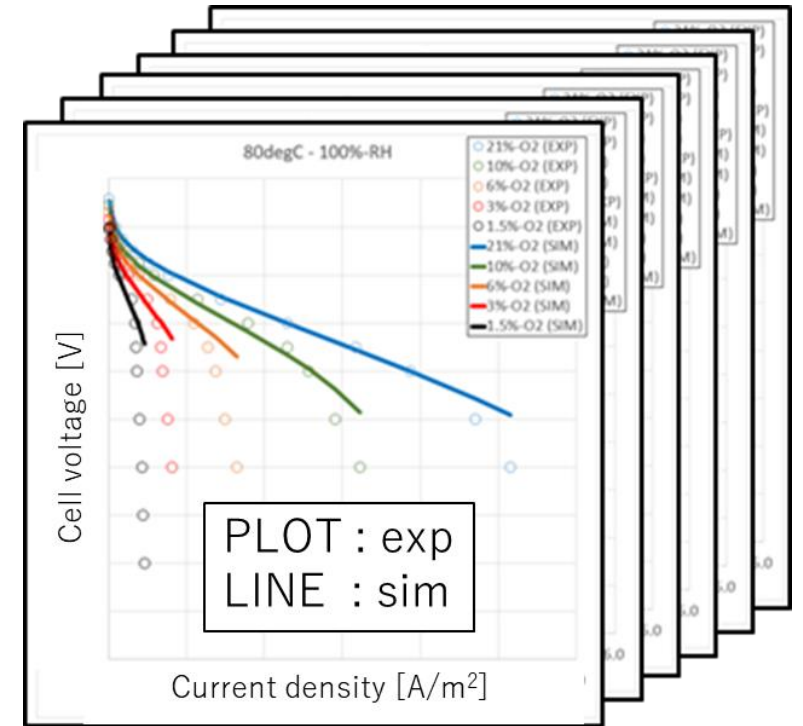
FC stack



Single cell ($\doteq 300 \text{ cm}^2$)

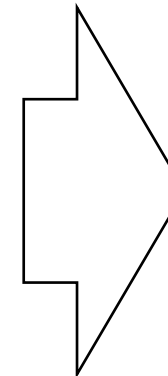
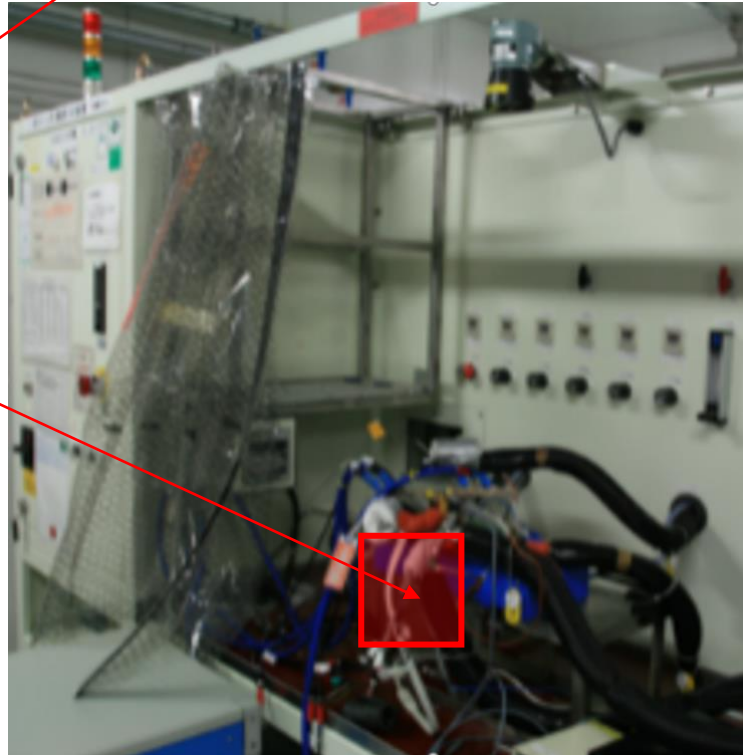
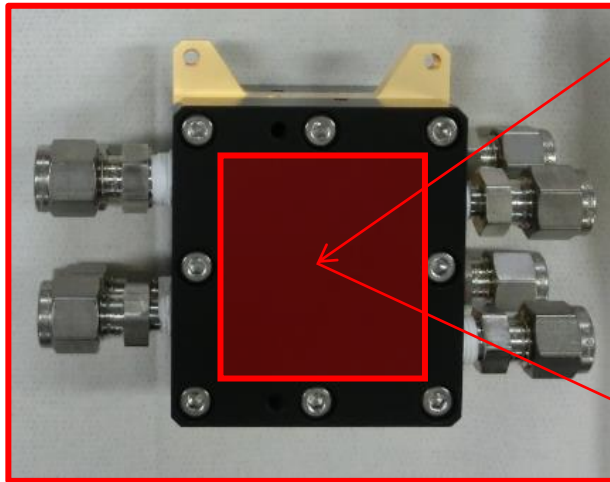


Experimental data



Test piece (1 cm^2)

Test bed



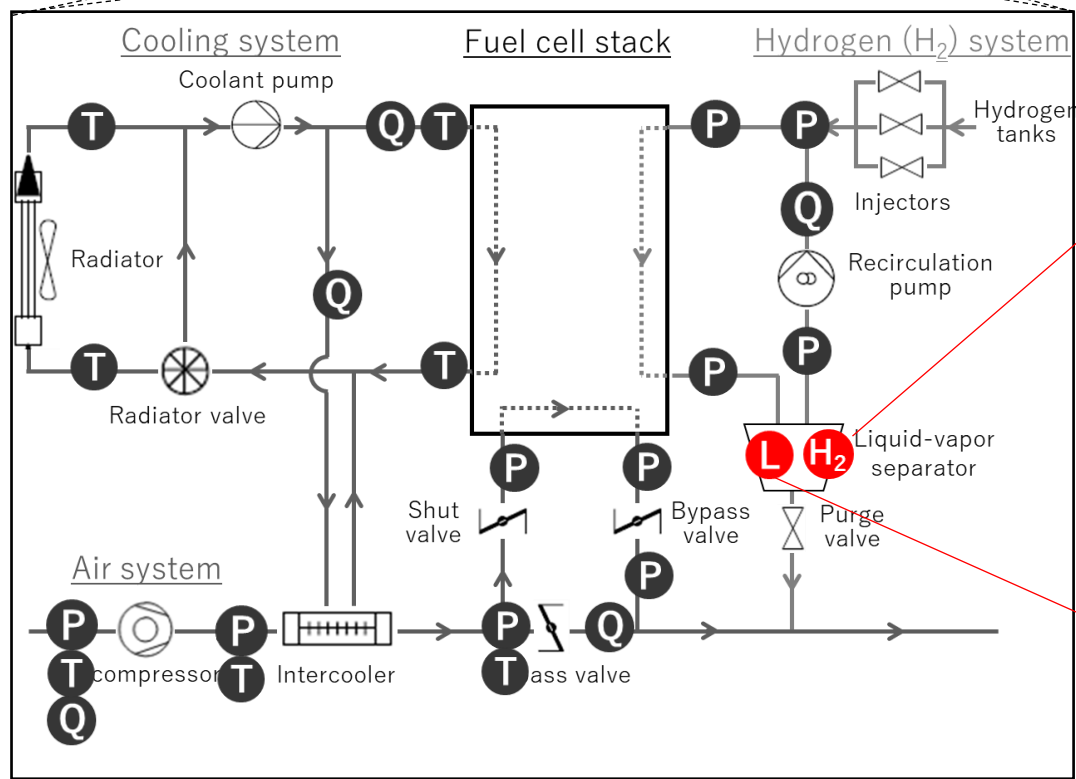
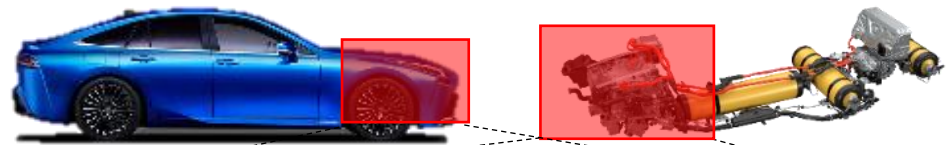
Boundary condition of 1 cm^2 -cell

- 5 humidity (100, 80, 60, 40, 20%)
- 5 O₂ concentration (21, 10, 6, 3, 1%)
- 3 coolant temperature (80 + 40, 60 °C)

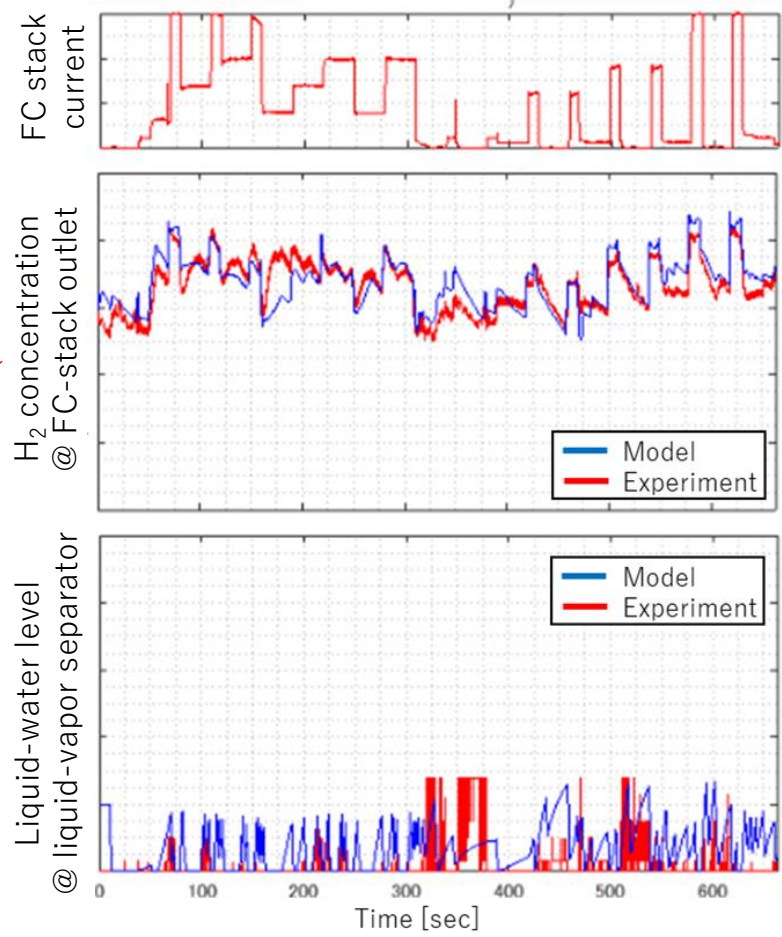
All the parameters can be determined with 1 cm^2 -cell data and microscopic observations of material geometries (**NOT** cell/stack data)

4. Model validation & verification

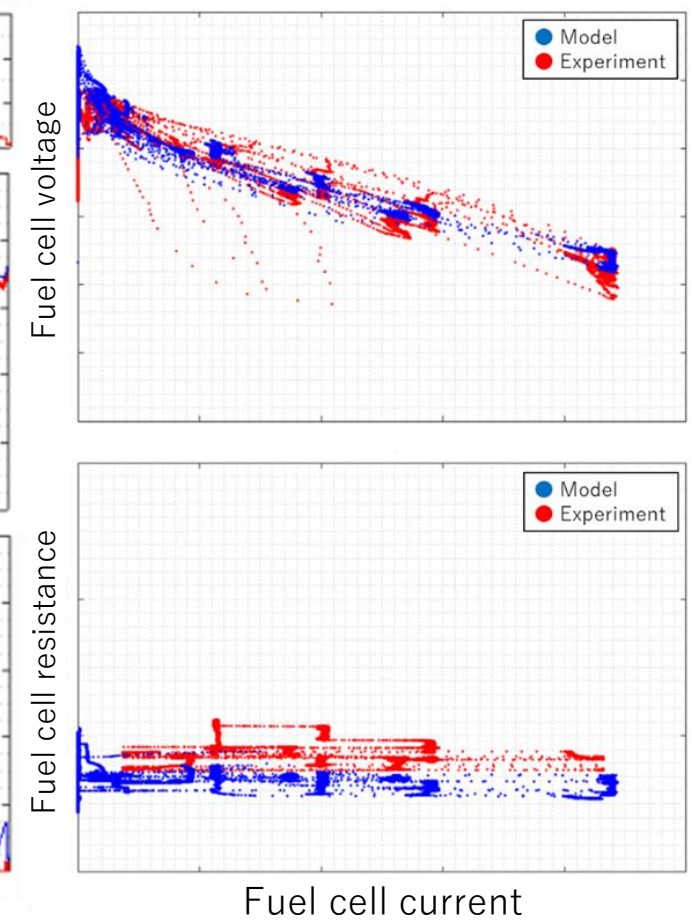
Prototype vehicle & system testbed w/additional sensors for validation



System dynamics (H₂ system)



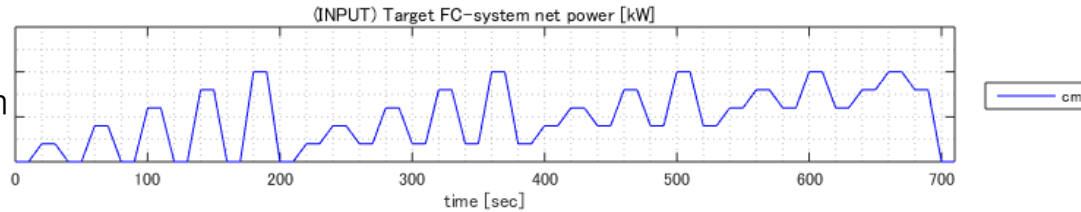
FC stack dynamics



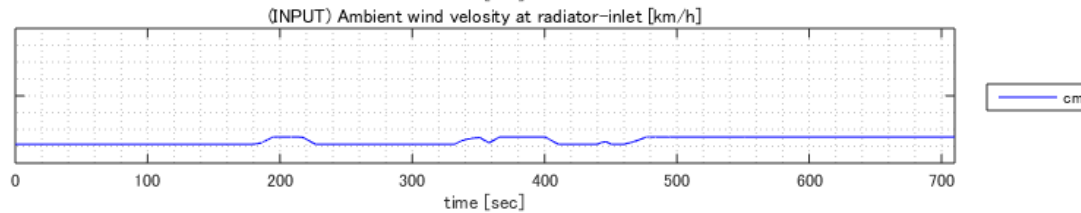
Validated with the database collected with prototype vehicle in wide range of conditions under low to high load and temperature

5. Simulation results : System dynamics in an entire FC-system

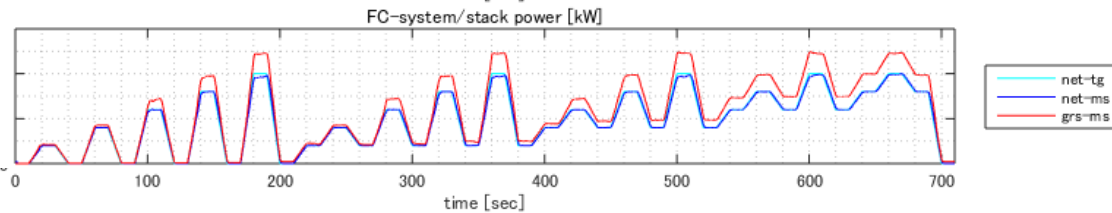
(Input)
Target FC-system net power



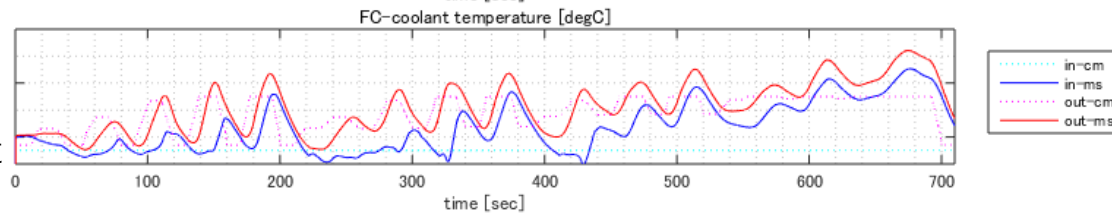
(Input)
Wind velocity at radiator inlet



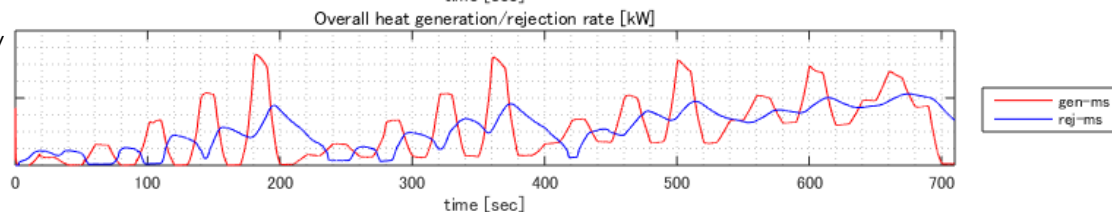
Target tracking performance / FC gross power



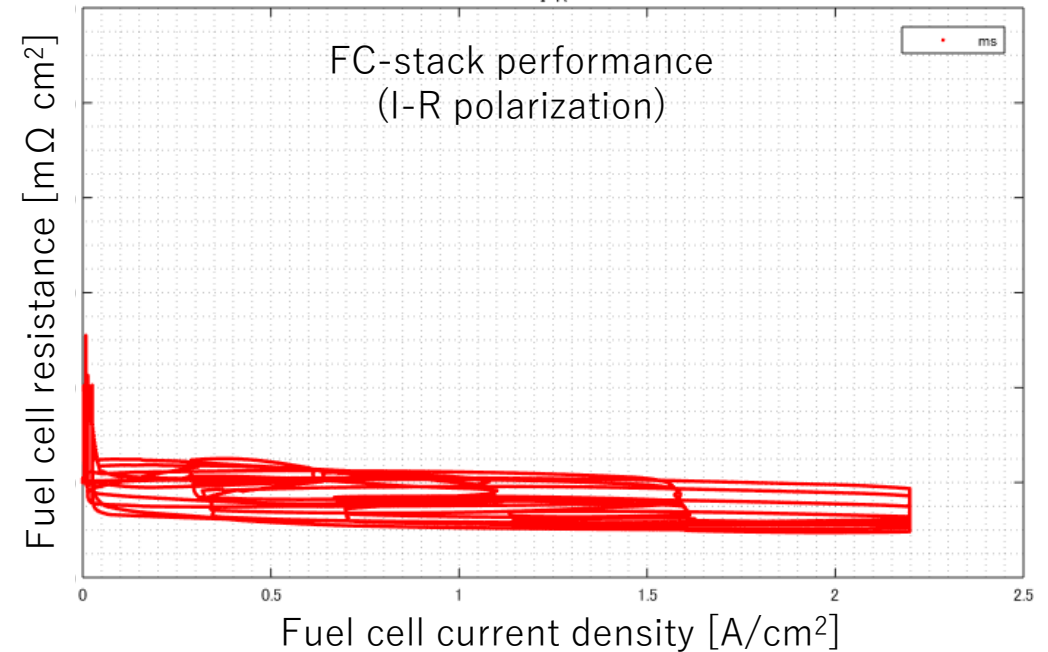
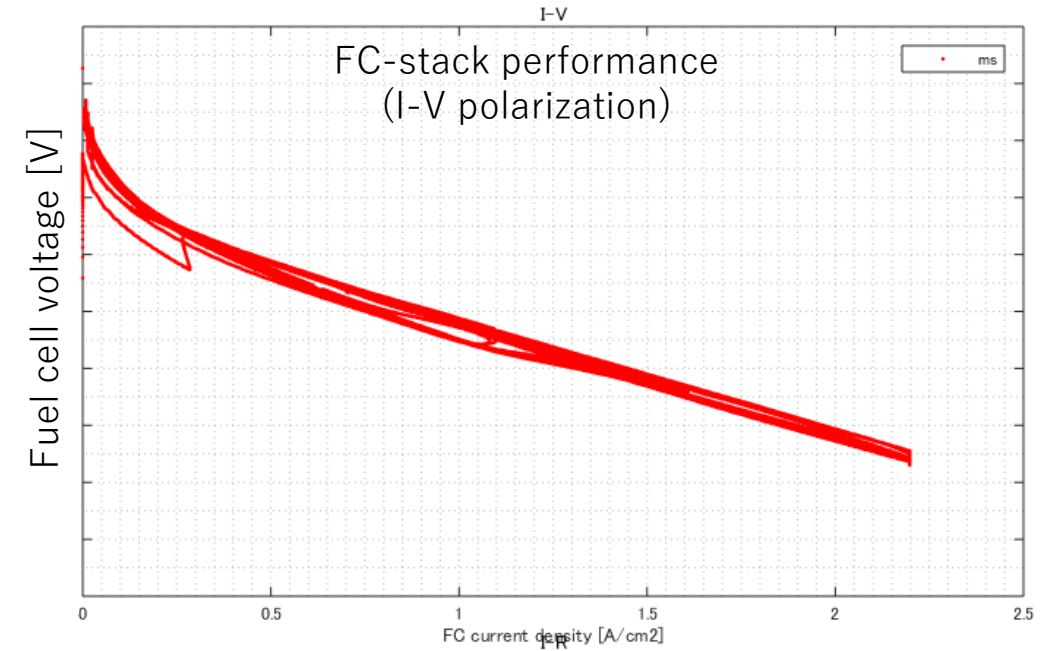
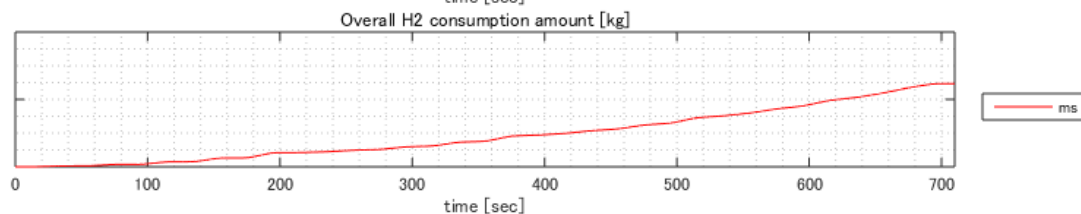
Coolant temperature at FC-inlet/outlet



Heat generation / emission rate in FC-system



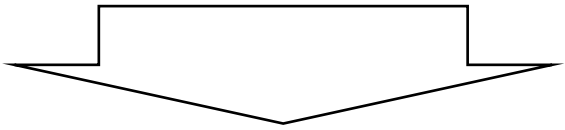
Accumulated H₂ consumption amount



5. Simulation results : Computational speed

Summary of computational speed

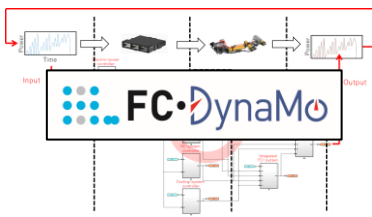
Hardware	CPU	Intel® Xeon® CPU E3-1230 v5 @ 3.40GHz, 3.41GHz
	RAM	8.00 GB
Software	OS	Windows 10® Enterprise
	MATLAB®	R2015a (8.5.0.197613)
	SIMULINK®	Version 8.5 (R2015a)
Experimental data	Total time	700 sec
	Number of data	42724 time-steps (0.016384 sec/step)
Computational time		13.2 sec



> 50 times
faster than
real-time

Capability of year-long durability simulation in allowable computational time

Being delivered to Japanese FCS manufacturers



- Year-1
- Year-2
- Year-3

Hardware models

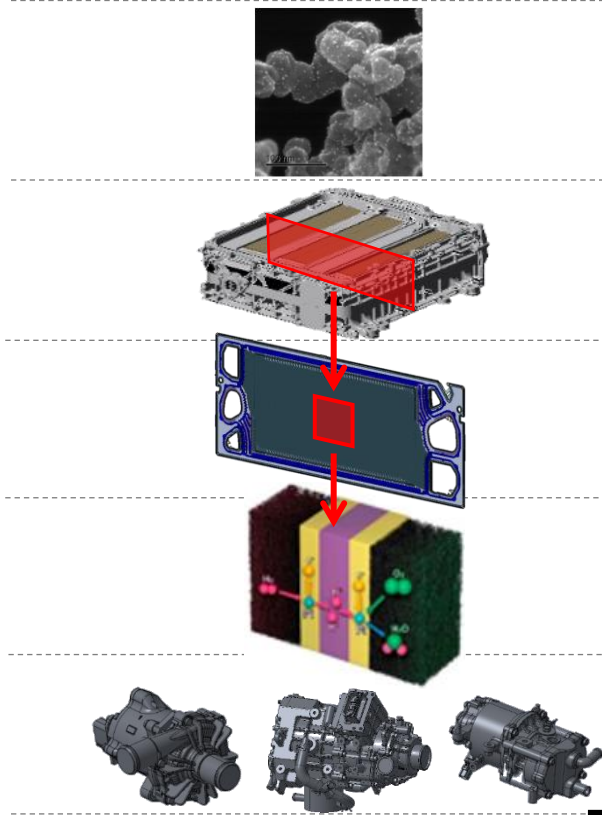


Controllers



GUI									
FC-stack (degradation)				FC-stack (degradation avoidance)					
Catalyst (platinum)	Catalyst (carbon)	Membrane (chemical)	Membrane (Mechanical)	Catalyst (platinum)	Catalyst (carbon)	Membrane (chemical)	Membrane (Mechanical)		
FC-stack (1+1+1D : stacking direction)				FC-stack					
Mass transport		Electrochemistry							
FC-stack (1+1D : In-plant direction)				FC-stack					
Mass transport		Electrochemistry							
FC-stack (1D : Through-plane direction)				Power		Fuel economy		Cooling	
Mass transport		Electrochemistry		FC-system					
FC-system									
Air	H2	Cooling	Electric power	Air	H2	Cooling	Electric power		

Target of Year-2 and 3



Platform : 


For detailed information

Sep. 2022

Modeling of overall fuel cell system dynamics

ECS Transactions

Modeling of the dynamic behavior of an integrated fuel cell system including fuel cell stack, air system, hydrogen system, and cooling system

Shigeki Hasegawa¹, Yoshihiro Ikogi², Sanghong Kim³, Miho Kageyama⁴ and Motoaki Kawase⁴ 

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[ECS Transactions, Volume 109, Number 9](#)

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Sep. 2021

Modeling of fuel cell stack dynamics

ECS Transactions

Modeling of Fuel Cell Stack for High-Speed Computation and Implementation to Integrated System Model

Shigeki Hasegawa^{1,2}, Motoyuki Kimata³, Yoshihiro Ikogi¹, Miho Kageyama², Motoaki Kawase²  and Sanghong Kim⁴

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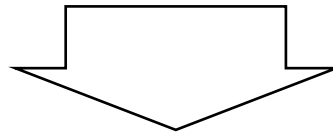


Conclusions

1D physical model for integrated fuel cell system,  **FC-DynaMo** as developed to enable year-long simulation of an entire fuel cell system dynamics in allowable calculation time

Accomplishments

- Function-block modeling & implementation methods
- Parameter determination process without collecting system-scale data
- x50 computational time than real time
- Validation by the database collected with commercial FCEV



Future work

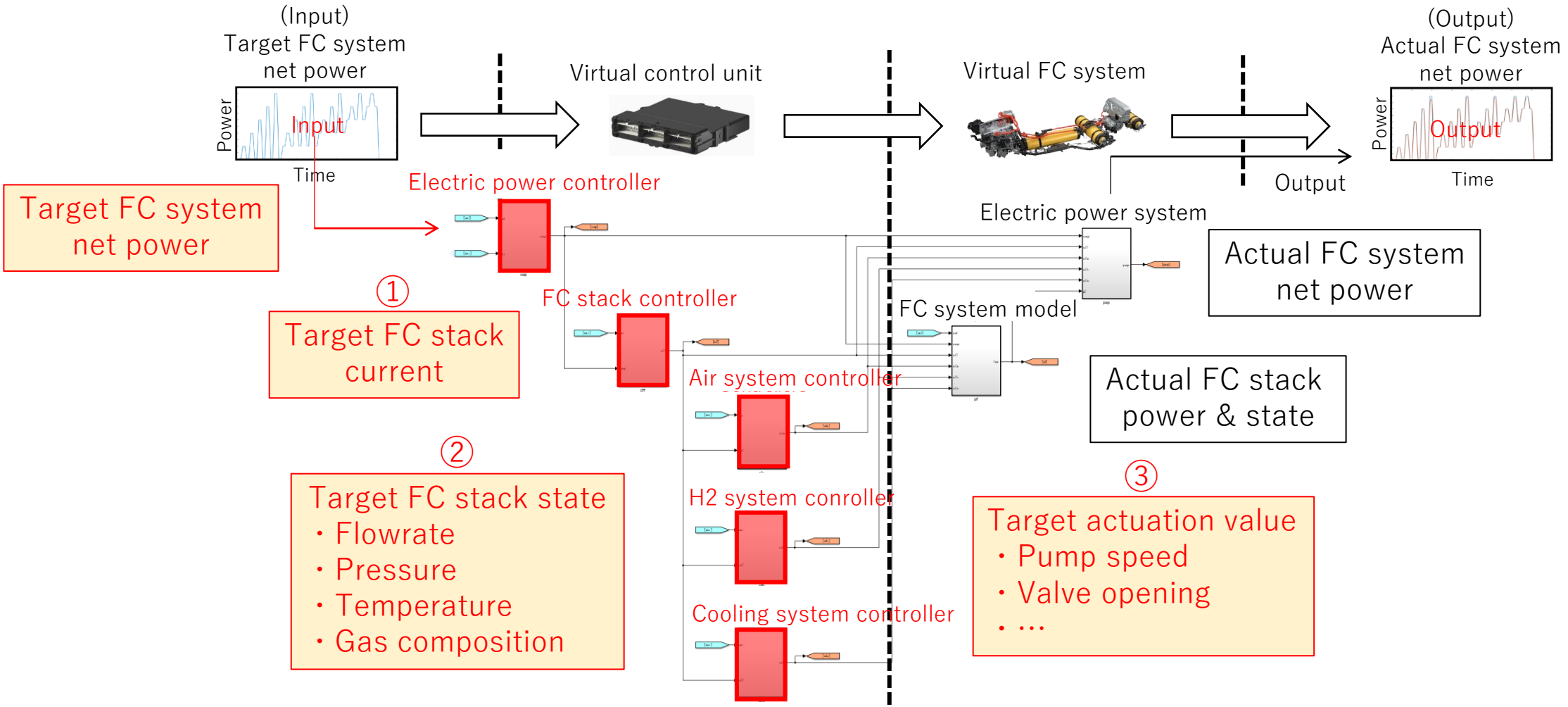
- Implementation of degradation models of FC materials for HDV application
- Extension of FC stack models to 1+1D and 1+1+1D directions

Acknowledgement

Appendix

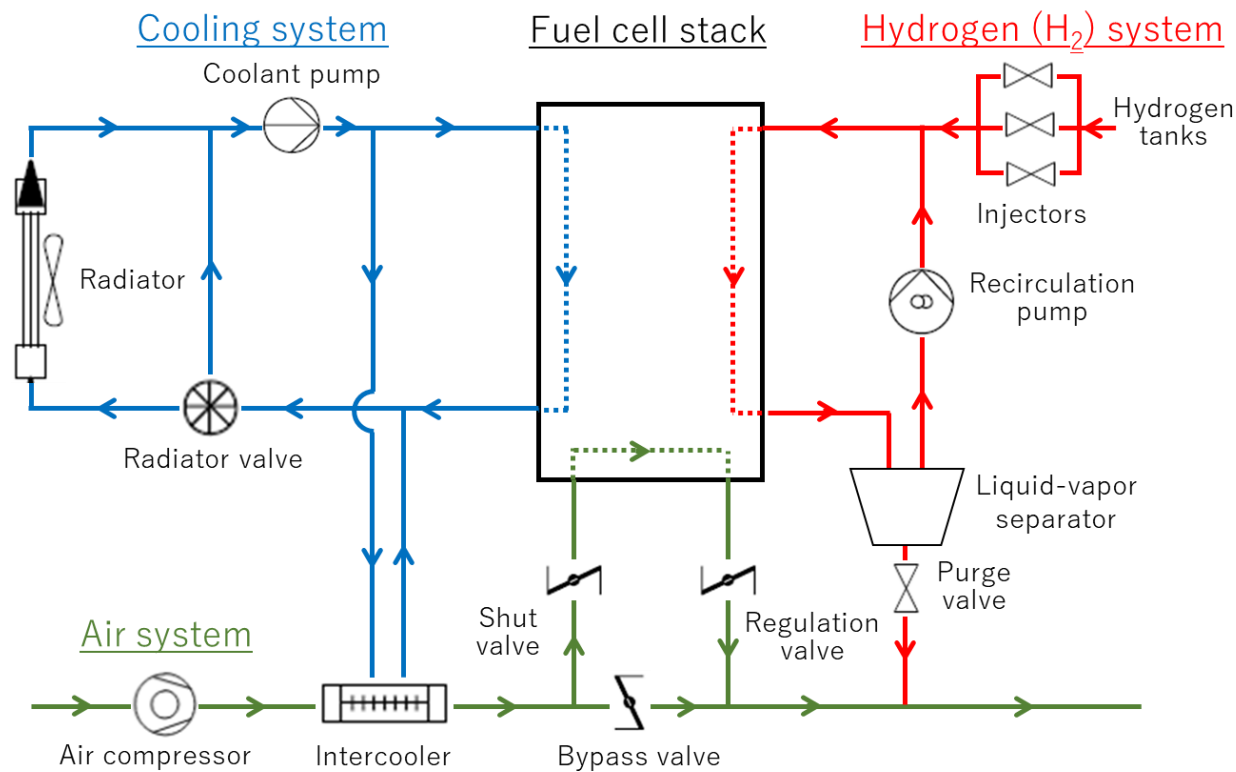
Controllers : Overview

3-step controller architecture, conversion of target power → state → actuation value
 ‘LEGO-BLOCK’ implementation for separation of calibration process and easy implementation



Controllers : Overview

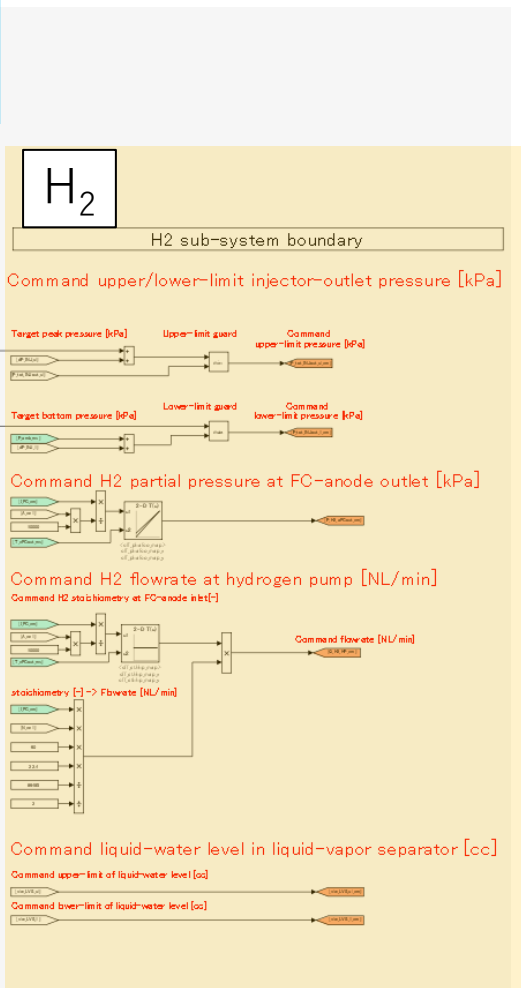
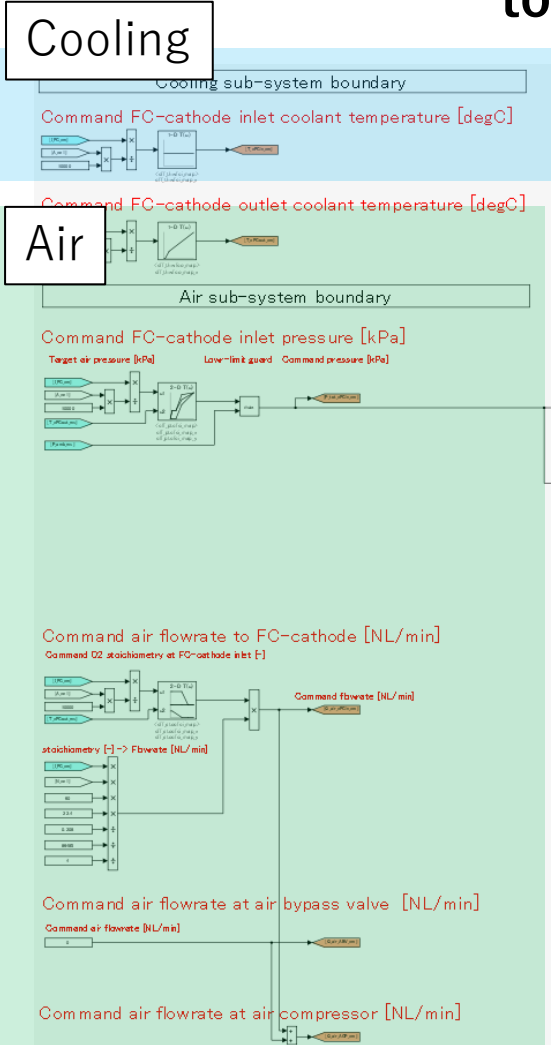
Role of each system component defined to achieve target power tracking in high FC system efficiency



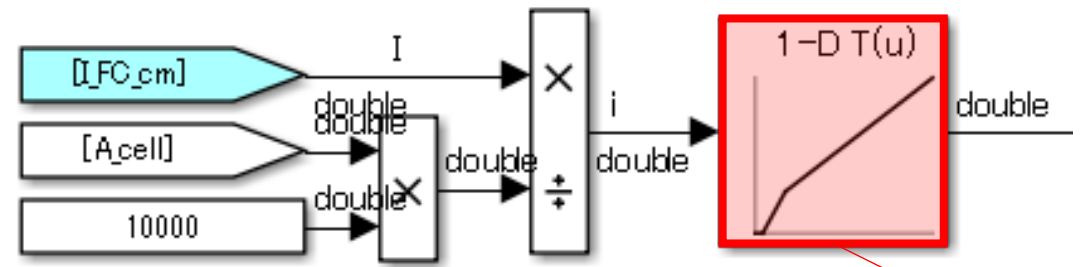
	ユニット	制御対象
Air	Air compressor	Total air flowrate
	Regulation valve	Air pressure
	Bypass valve	Bypass air flowrate
	Shut valve	Sealing in shut-down condition
H ₂	Injector	H ₂ partial pressure
	Purge valve	H ₂ partial pressure
	Recirculation valve	Circulation flowrate
	Liquid-vapor separator	Removal of water droplets
Cooling	Coolant pump	FC stack outlet temperature
	Radiator valve	FC stack inlet temperature
	Radiator + fan	Boosting radiator performance

Controllers : FC stack controller

Optimized FC stack boundary condition of flowrate, pressure, temperature, and composition to achieve target power tracking in high system efficiency



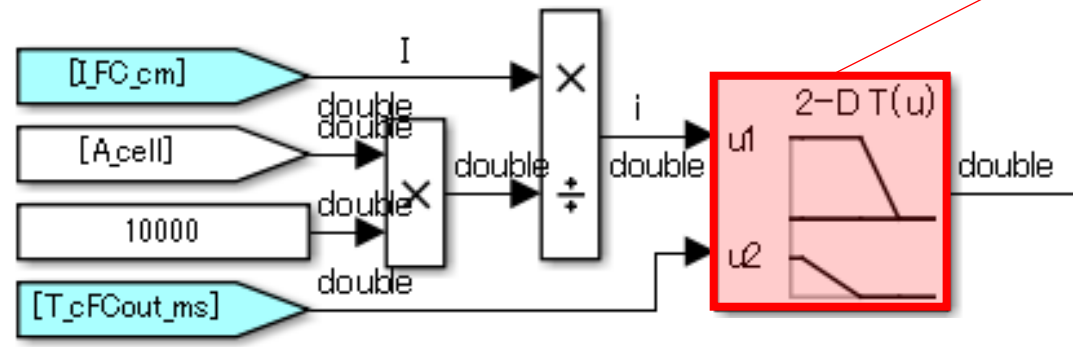
(Ex : Cooling) Target coolant temperature



Input : FC current

Predetermined functions

(Ex : Air) Target air flowrate



Input : FC current + temperature

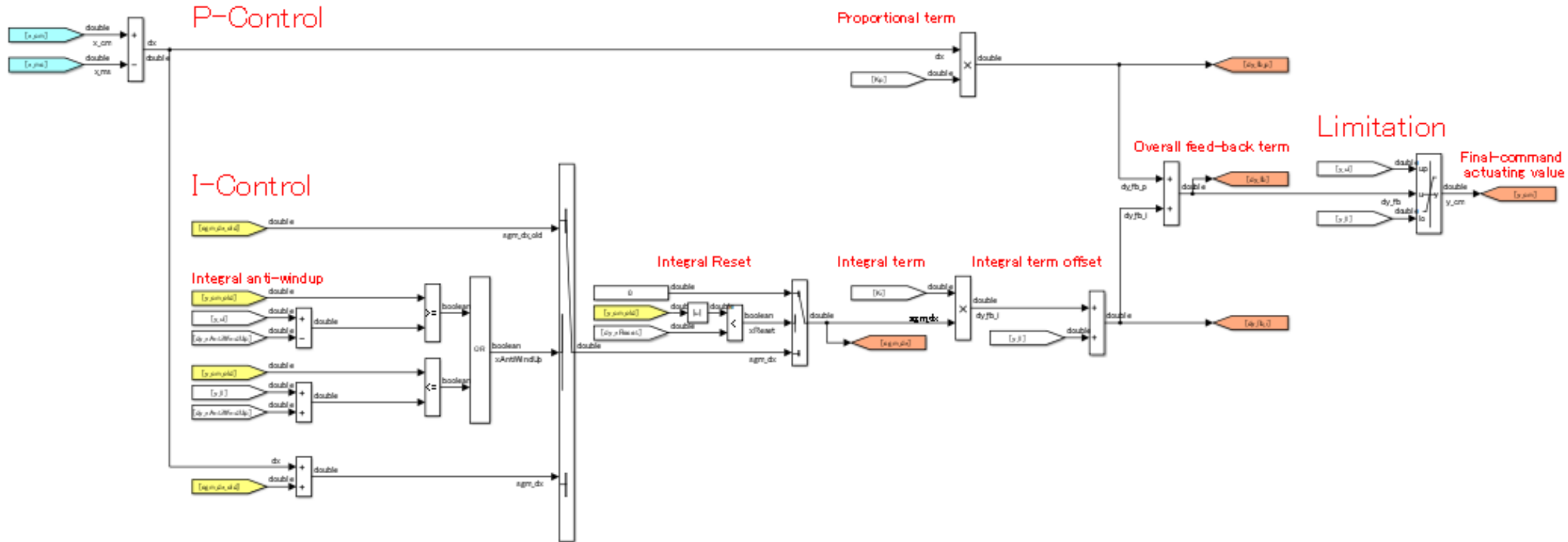
- Operating conditions are calibrated and implemented as table data
- Separation of FC stack & components controller calibration process ('LEGO-BLOCK' implementation)

Controllers : FC system component controller

(Ex : Air) Air compressor speed controller

Input : Target flowrate

Output : Target speed

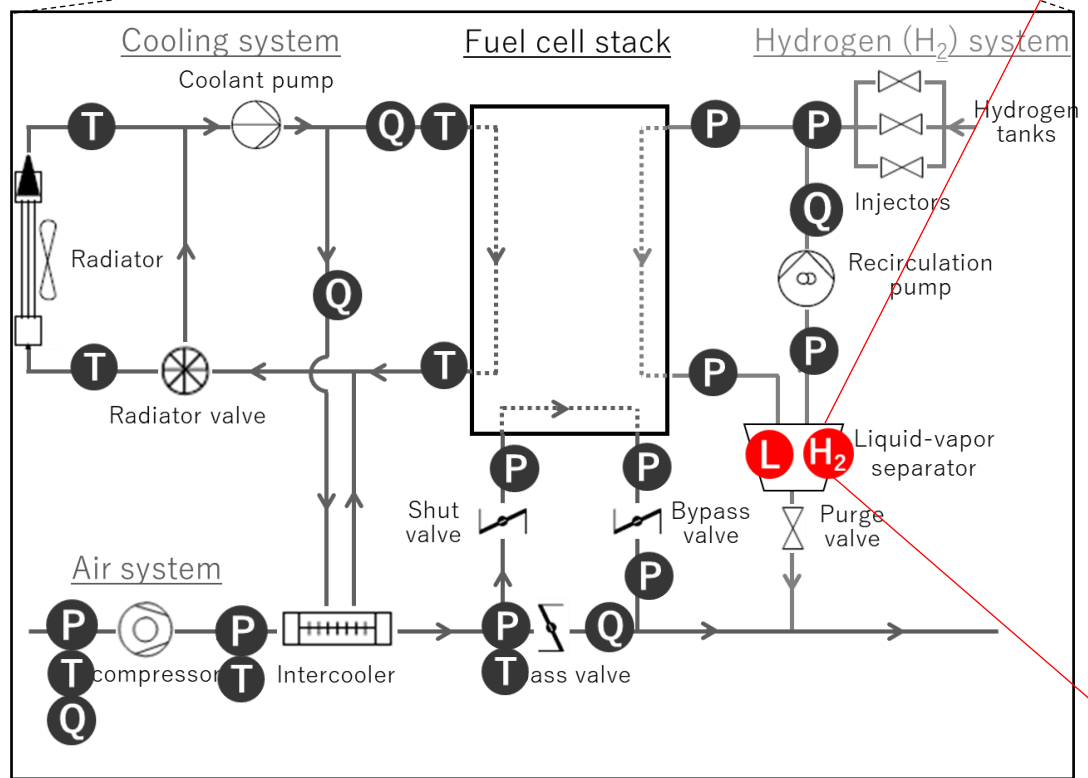


- Simple SISO PI controller, various component characteristics can be expressed by only PI gain tuning
- More sophisticated controller such as MPC can be implemented by replacing original controller without large effort ('LEGO-BLOCK' implantation)

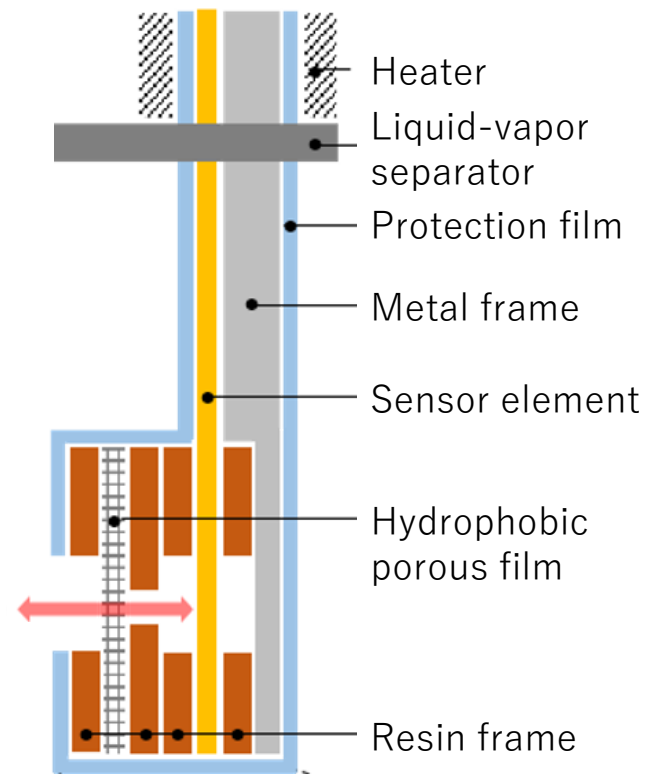
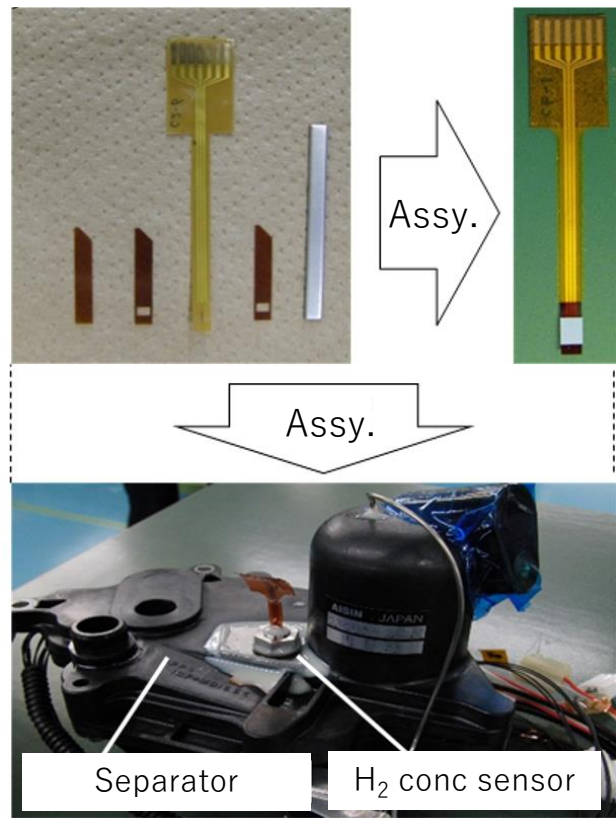
Model validation

Following the packaging limitation to install additional sensors, compact and accurate sensors were newly developed

Prototype vehicle
w/additional sensors for validation



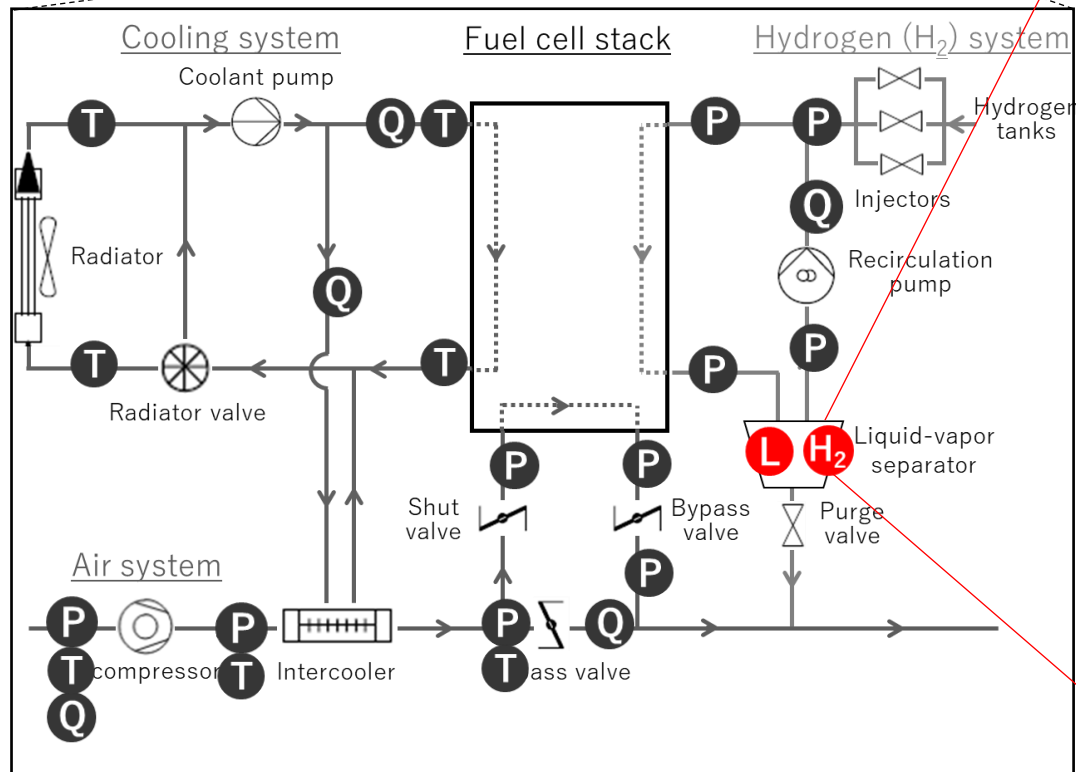
H₂ concentration sensor



Model validation

Following the packaging limitation to install additional sensors, compact and accurate sensors were newly developed

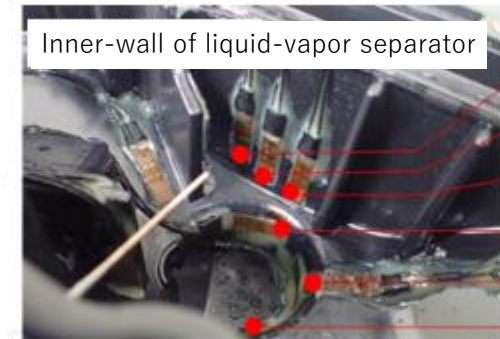
Prototype vehicle w/additional sensors for validation



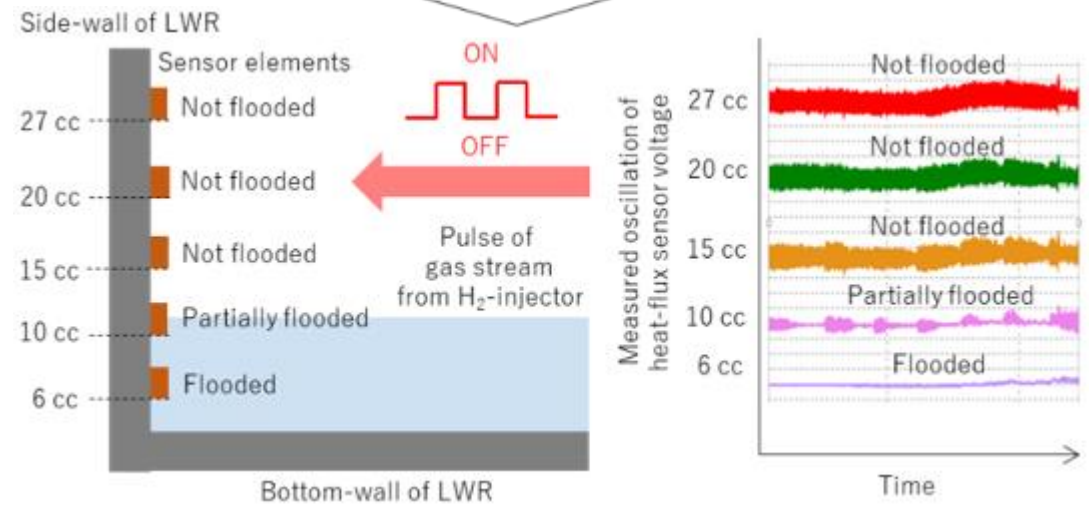
Liquid-level sensor



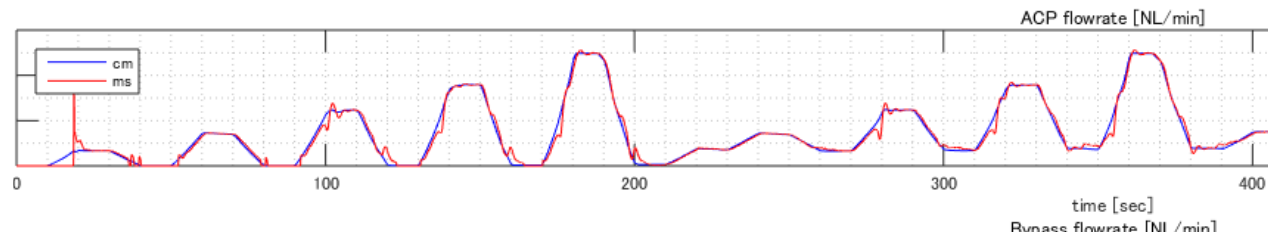
Assemble



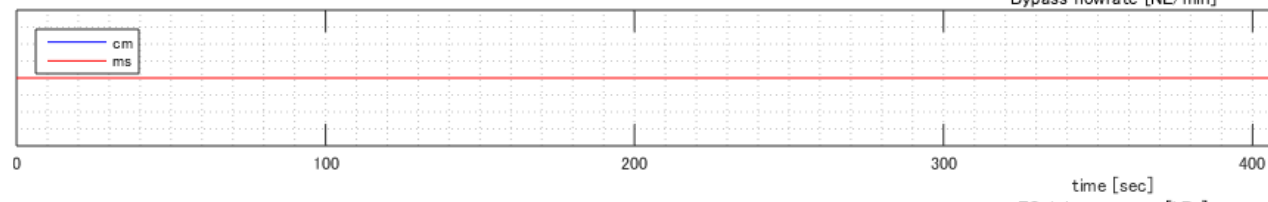
Integrate



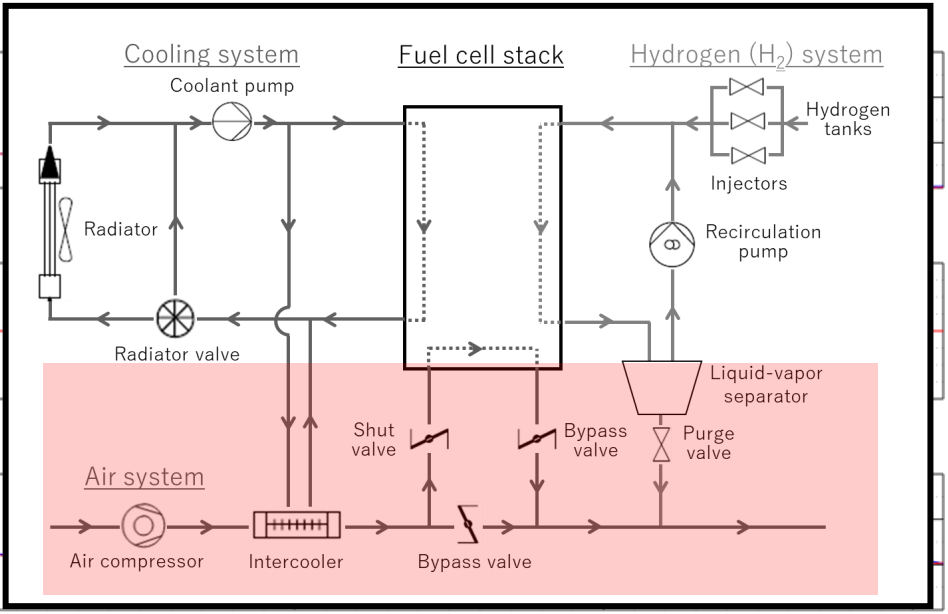
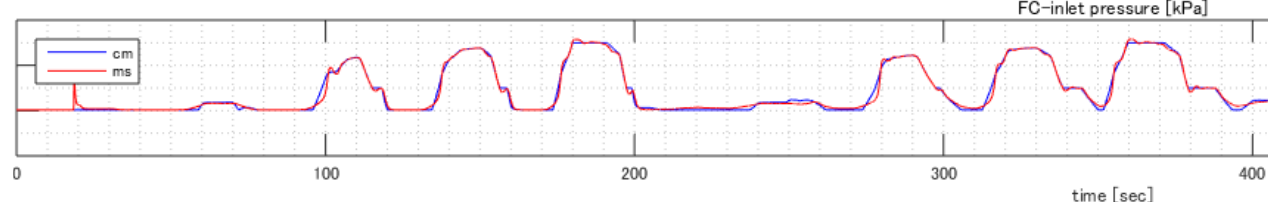
Air compressor flowrate (cm/act)



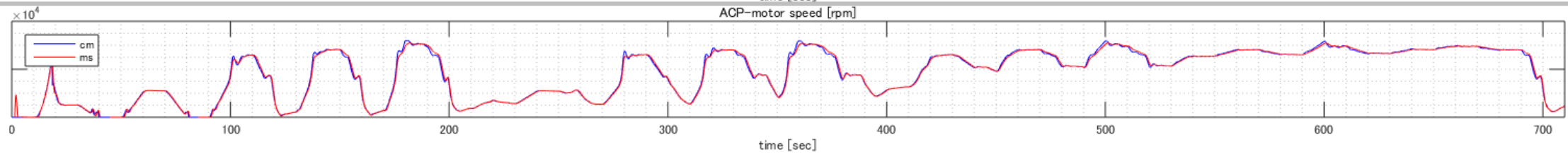
Air flowrate at bypass line (cm/act)



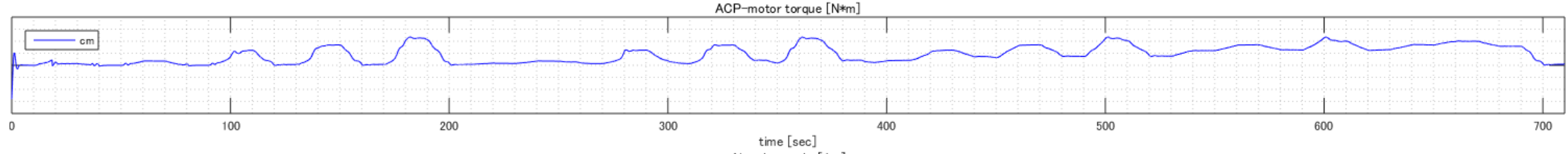
Total pressure at FC-stack inlet (cm/act)



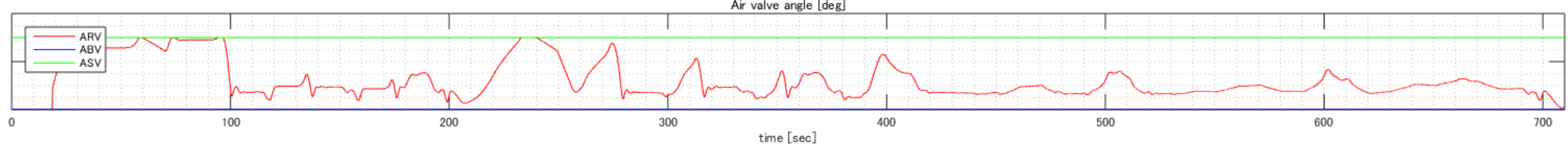
Air compressor rotational speed (cm/act)



Air compressor motor torque (cm/act)

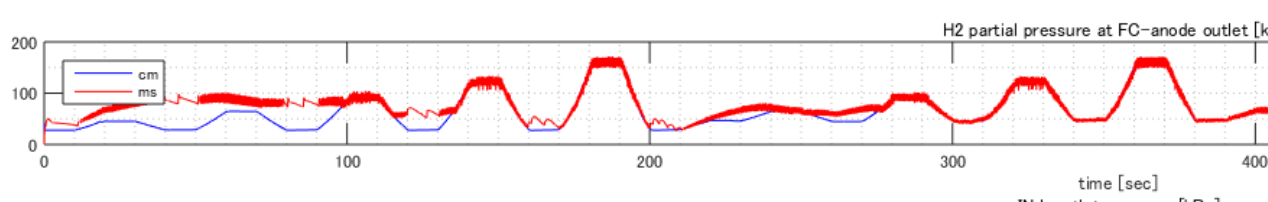


Air valve opening

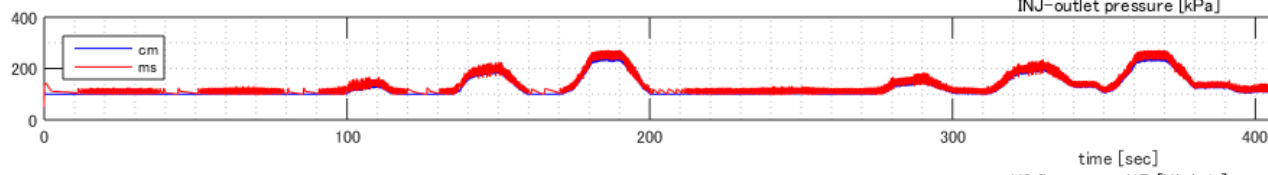


Model output : H₂ system dynamics

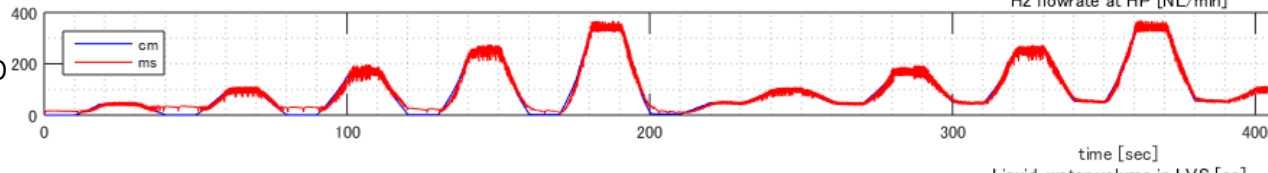
H₂ partial pressure at FC-stack outlet (cm/act)



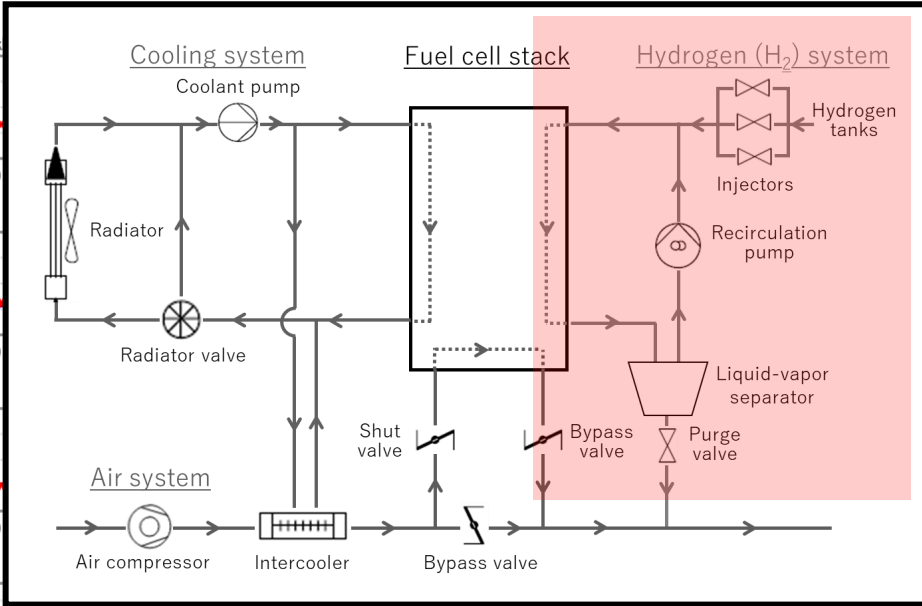
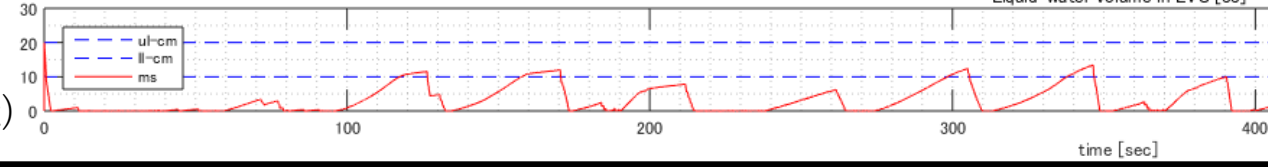
Total pressure at Injector outlet (cm/act)



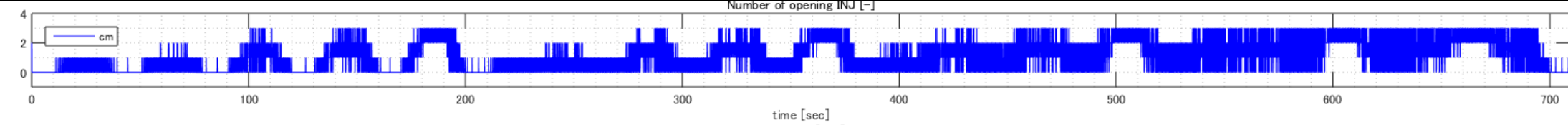
H₂ flowrate at recirculation pump (cm/act)



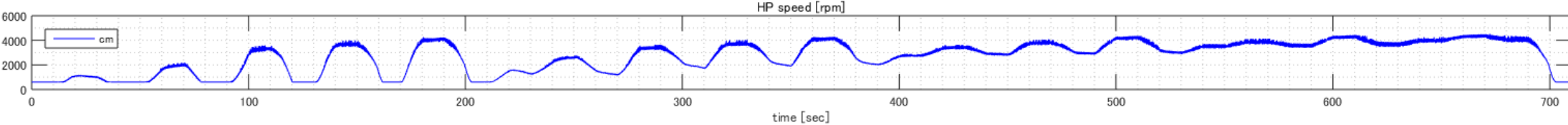
Water level at liquid-vapor separator (cm/act)



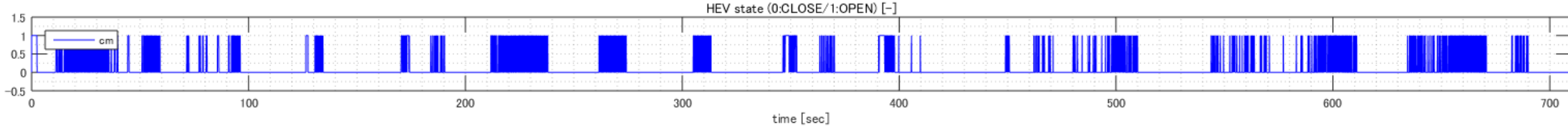
Opening injector count



Recirculation pump speed

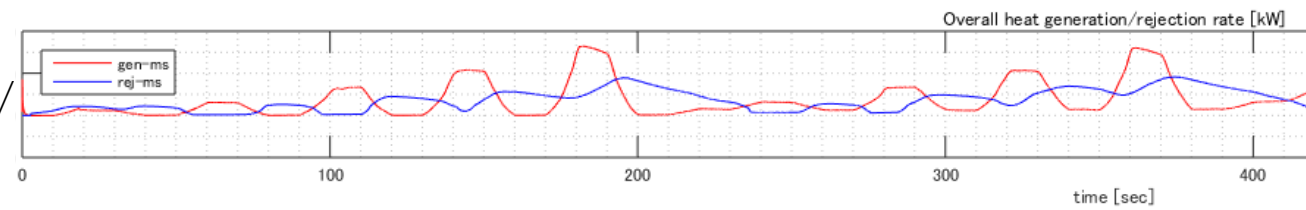


Purge valve state (open/close)

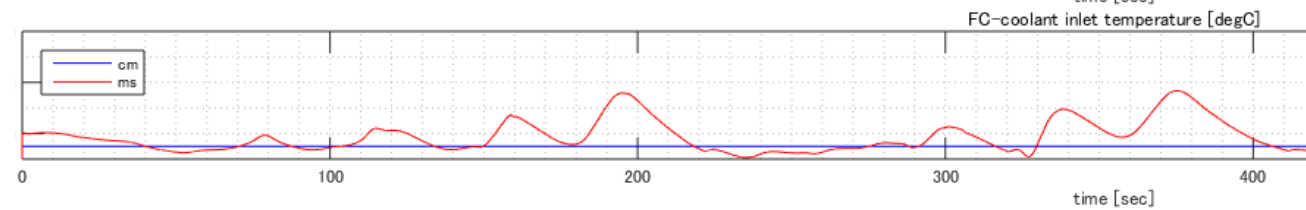


Model output : Cooling system dynamics

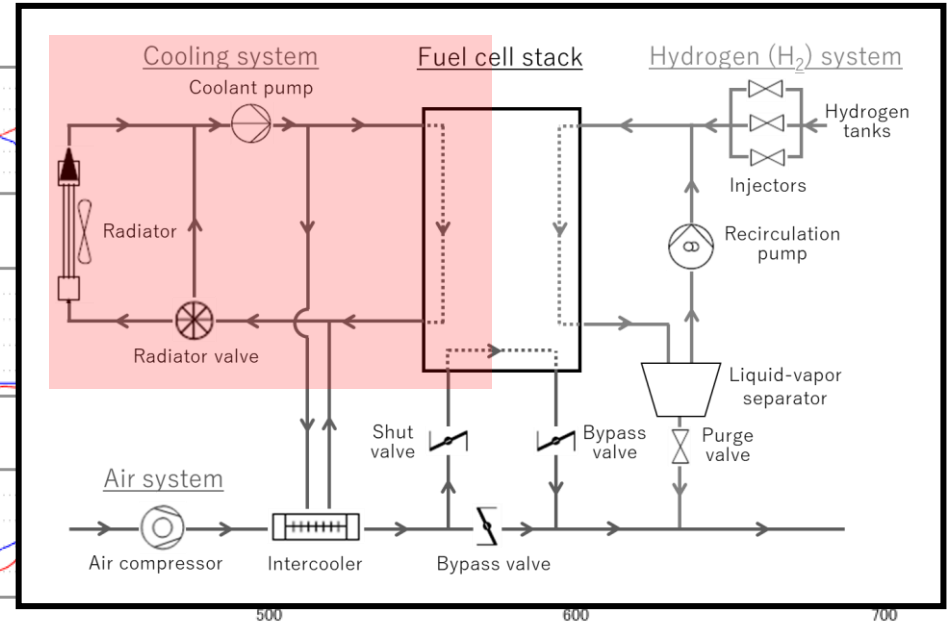
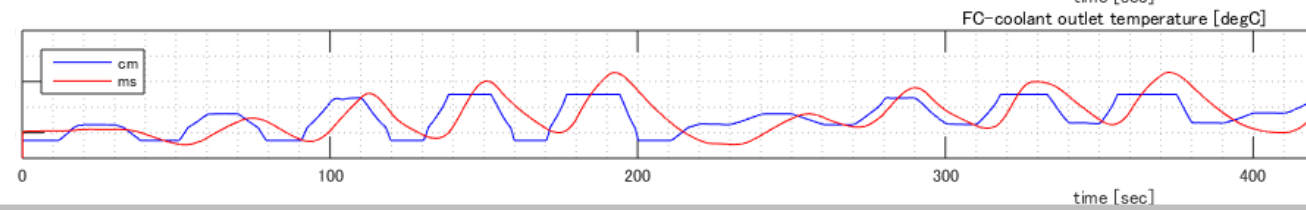
FC-system heat generation / radiation rate



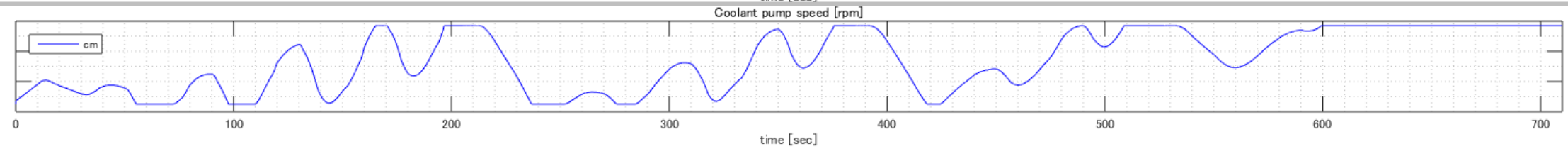
Coolant temperature at FC-stack inlet



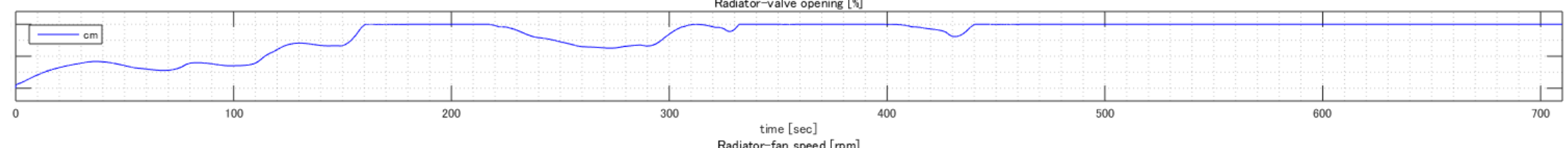
Coolant temperature at FC-stack outlet



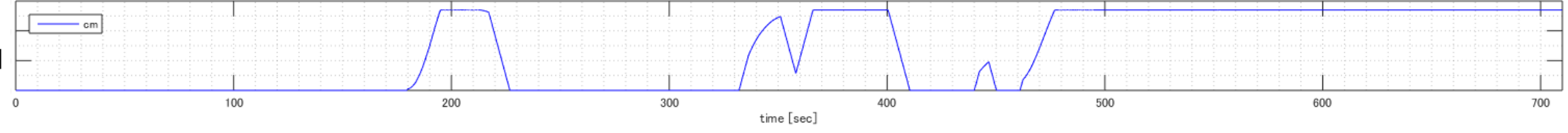
Coolant pump speed



Radiator valve opening

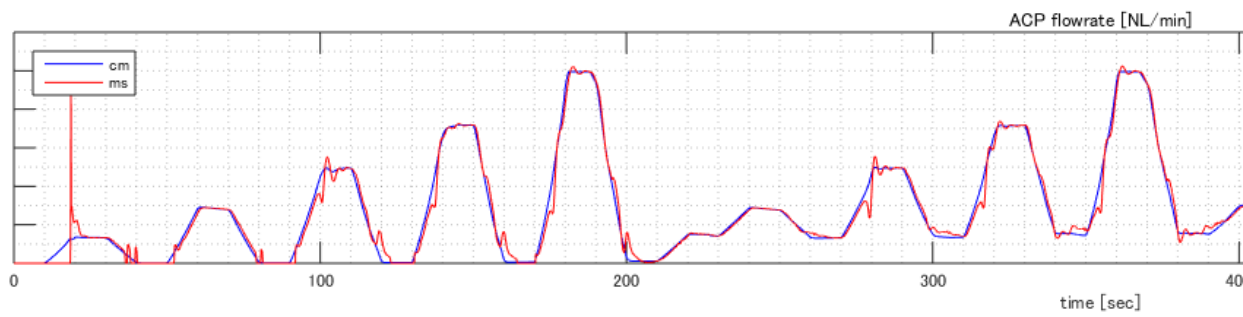


Radiator fan rotational speed

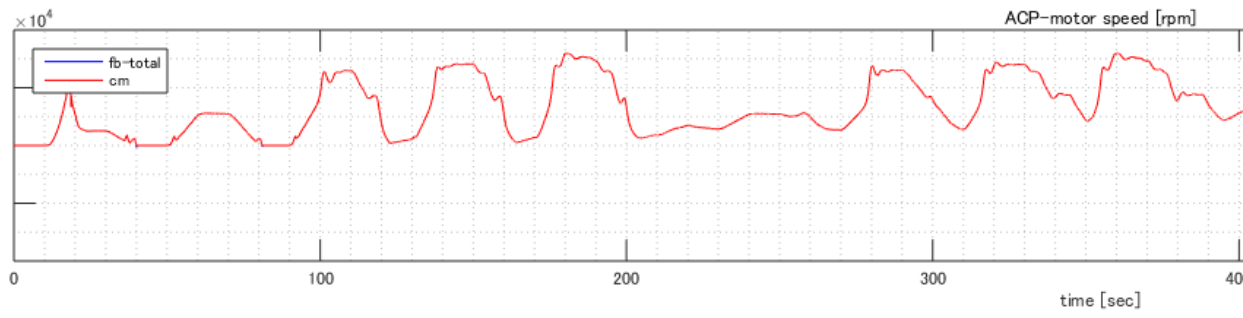


Model output : Air system controller

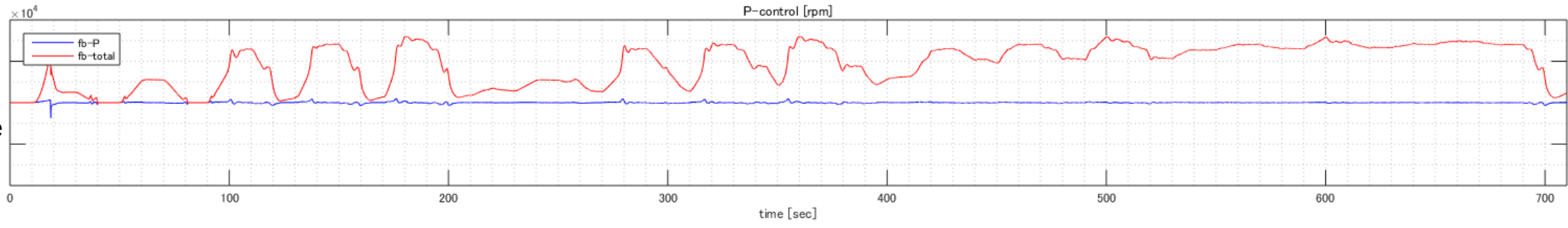
Air compressor rotational speed (cm/act)



Air compressor flowrate (cm/act)



Contribution of P-control for command value



Contribution of I-control for command value

