Code Verification and Run-Time Error Detection Through Abstract Interpretation

A Solution to Today’s Embedded Software Testing Challenges

Testing embedded systems is a difficult task, made more challenging by time pressure and the increasing complexity of embedded software. To date, there have been basically three options for detecting run-time errors in embedded applications: code reviews, static analyzers, and trial-and-error dynamic testing. Code reviews are labor-intensive and often impractical for large, complex applications. Static analyzers identify relatively few problems and, most importantly, leave most of the source code undiagnosed. Dynamic or white-box testing requires engineers to write and execute numerous test cases. When tests fail, additional time is required to find the cause of the problem through an uncertain debugging process.

Abstract interpretation takes a different approach. Instead of merely detecting errors, it automatically verifies important dynamic properties of programs—including the presence or absence of run-time errors. It combines the pinpoint accuracy of code reviews with automation that enables early detection of errors and proof of code reliability. By verifying the dynamic properties of embedded applications, abstract interpretation encompasses all possible behaviors of the software and all possible variations of input data, including how software can fail. It also proves code correctness, providing strong assurance of code reliability. By using testing tools that implement abstract interpretation, businesses can reduce costs while accelerating the delivery of reliable embedded systems.

This paper describes how abstract interpretation works and how you can use it to overcome the limitations of conventional techniques for testing embedded software.

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Challenges in Testing Embedded Software

As processing power and memory costs have decreased, embedded software applications have penetrated virtually every industrial sector, from consumer electronics and appliances to aerospace, defense, automotive, avionics, telecommunications, and medical devices. Over the past several years, strong demand for complete, multi-purpose software applications has led to much larger and more complex embedded systems. In some industries, the quantity of embedded software doubles every 18 months. Even as the number and complexity of these applications grow, the safety-, mission-, life- or business-critical aspects of many embedded applications continue to demand high levels of reliability and robustness.
Market pressure affects any software development. An application under development is subject to constant changes, including specification updates and design changes. Development organizations must often meet conflicting business objectives: deliver higher quality embedded software while reducing time-to-market. The challenge is increased by the complexity of the applications being developed and the frequent shortage of engineering resources.

One solution is to improve efficiency by using software tools for code generation, design, and code instrumentation. These tools have enabled embedded software development teams to do more in less time. However, testing and debugging tools have not kept pace with the increases in embedded software size and complexity. As a result, the cost of testing an embedded system today can be up to 50% of total development costs.

Early code verification is an effective way to relieve time and cost pressures. Indeed, errors detected in the late phases of the development cycle are more difficult to debug because they must be traced back to their source among tens or hundreds of thousands of lines of code, often by testers who did not write the code themselves. The cost of fixing problems found late in testing is 10- to 20-fold higher than the cost of fixing the same errors during coding.

While early code verification offers clear benefits, it is still the exception rather than the rule. For many teams, this means that testing is done close to the project’s deadline, when time pressure is at its highest. In this environment, run-time errors, which are typically among the most difficult to find, can be missed altogether. These errors, caused by arithmetic and other anomalies in the code (divisions by zero, out-of-bound arrays, illegal dereferencing of pointers, read access to non-initialized data, and so on), are also known as latent faults because they are not readily apparent under normal operation. Software developers find that up to 40% of bugs detected in software applications during maintenance are run-time errors. These errors may cause non-deterministic behavior, incorrect computations (such as integer overflow), or processor halt due to arithmetic exception. They all have unpredictable, sometimes even dramatic, consequences on the reliability of the application.

Limitations of Common Run-time Error Detection Techniques

The methods and tools conventionally used to detect and debug run-time errors rely on technology that is 20 to 30 years old. These approaches fall into three broad categories: manual code reviews, static analyzers, and dynamic, or white-box, testing. Those techniques focus on finding errors. They are unable to prove the absence of errors.

**Manual code review** can be an effective technique for finding run-time errors in relatively small applications (comprising 10-30k lines of code). For larger systems, however, manual review is a labor-intensive process. It requires experienced engineers to review source code samples and report dangerous or erroneous constructs, an activity that is complex, non-exhaustive, non-repeatable, and costly. Proving the absence of run-time errors is a much complex operation that is not manageable by code review.

**Static analyzers** provide very limited support for run-time error detection. Compilers, linkers, quality measurement tools (for example, tools that report on comment rate, call-graph depth, or the code structure complexity) can only detect errors that do not depend on program execution—for example, static expressions composed of constants and literal values (such as static overflow), static division by a constant expression equal to 0, and explicitly non-initialized data. Other run-time errors, such out-of-bound array access, conditionally initialized data, and illegal dereferencing of pointers, are beyond the scope of such tools.

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Dynamic testing or white-box testing requires engineers to write and execute test cases. Thousands of test cases may be required for a typical embedded application. After executing a test case, the test engineer must review the results and trace errors back to their source. This testing process has not improved much in the last two decades. While engineers can take other steps to improve the chances of detecting anomalies, such as code instrumentation and code coverage, dynamic testing is based on a trial-and-error approach that provides only partial if not minuscule coverage of all the possible combinations of values that can be encountered at run time. Like manual code reviews, the process is resource- and time-intensive. Time spent writing the test cases and waiting for an executable system to be developed often forces dynamic testing to be delayed until the end of the development cycle, when errors are most expensive to fix.

Engineers who use dynamic testing to find run-time errors in embedded applications face other challenges as well. First, testing costs increase exponentially with the size of the application. Since the number of errors tends to be constant for a fixed number of lines of code (a conservative estimate is 2 to 10 errors per 1,000 lines), the chance of finding these errors greatly decreases as the total number of lines in a software application increases. When the size of source code is doubled, the testing effort generally must be multiplied by four or more to obtain the same level of confidence as before.

Second, dynamic testing identifies only symptoms, not the cause, of the error. As a result, additional debugging time must be spent to localize the cause of each error after it has been detected during program execution.

Tracing an anomaly back to its root cause in the code can be extremely time-consuming when the defect is detected late in development. An anomaly detected in validation can take 100 hours to trace, while one caught in unit testing may be localized in an hour or less. While testing activities can be automated, debugging cannot. If every 1,000 lines of new code includes 2 to 10 errors, a 50,000 line application would contain a minimum of 100 errors. A developer spending an average of 10 hours debugging each error would need 1,000 hours to debug the application.

Third, dynamic testing frequently leads engineers to instrument their code so that anomalies can be observed more easily during program execution. But code instrumentation takes time, adds execution overhead, and can even mask errors, such as memory violation and access conflicts on shared data. Furthermore, methods based on code instrumentation detect errors only if the test cases that are executed raise an anomaly.

Fourth, the effectiveness of run-time error detection also depends on the ability of the test cases to analyze the different combinations of values and conditions that can be encountered at run-time. Test cases generally cover only a fraction of all possible combinations. This leaves a large number of untested combinations, including some that may cause a run-time error.

Error-Prevention and Fault-Tolerance Techniques

Some development languages provide exception-handling capabilities that can catch anomalies when they occur during execution, and let you decide whether the program should continue from a safety position, by recovery on a redundant computer, or by rebooting. These capabilities usually generate execution overhead, such as pre- and post-conditions as well as exception handlers, that which may not be compatible with the operational specifications of embedded applications.

As a result, test engineers sometimes activate them only during testing, removing them from the product before shipment. Run-time errors in a shipped product can cause serious, even catastrophic, results.
Another approach to preventing errors uses formal methods, such as theorem proving. While powerful, theorem proving is very intrusive and requires a high degree of mathematical expertise to be efficient, limiting its potential for use on industrial-scale applications.

**Code Verification with Abstract Interpretation**

Abstract interpretation bridges the gap between conventional static analysis techniques and dynamic testing by verifying the dynamic properties of software applications at compilation time. Without executing the program itself, abstract interpretation investigates all possible behaviors of a program – that is, all possible combination of values – in a single pass to determine how and under which conditions the program can fail. Abstract interpretation is a mature and sound mathematical approach. It can be seen as an extension of the compilation techniques used by programmers to predict how a software application will behave before performing actual tests.

**An Analogy from the Physical World**

An engineer who needs to predict the trajectory of a projectile in mid-air has three options:

- Make an exhaustive inventory of the different particles that will be on the projectile’s path, study their properties, and determine how impact with each particle will affect its trajectory. Obviously, this approach is impractical due to the huge number and variety of particles encountered during flight. Even if it was possible to know in advance all the conditions that could be encountered at any time (such as wind speed, and cloud drops), these would change for every new flight. This means a thorough analysis would need to be run again before every launch.

- Launch many projectiles to derive empirical laws of motion and related error margins. These findings can be used to estimate the trajectories within a certain confidence interval. This approach is both costly and time-consuming, however, and each attempt will change the conclusions. Furthermore, exhaustively testing the projectile under every possible combination of conditions is all but impossible.

- Use the laws of physics and known values (force of gravity, air braking coefficient, initial speed, and so on) to transform the problem into a set of equations that may be solved by mathematical rules, either formal or numeric. This approach produces solutions for a wide range of conditions that become parameters in the mathematical model, enabling the engineer to predict projectile behavior under a variety of conditions.

Abstract interpretation is like the mathematical modeling approach. It derives the dynamic properties of data from the software source code--that is, equations between variables--and applies them to the verification of specific dynamic properties.
**How Abstract Interpretation Works**

Abstract interpretation relies on a broad base of mathematical theorems that define rules for analyzing complex dynamic systems such as software applications. Instead of proceeding with the enumerative analysis of each state of a program, abstract interpretation represents these states in a more general form and provides the rules to manipulate them. Abstract interpretation not only produces a mathematical abstraction, it also interprets the abstraction.

To produce a mathematical abstraction of program states, abstract interpretation thoroughly analyzes all variables of the code. The substantial computing power required for this analysis has not been readily available in the past. Abstract interpretation, when combined with non-exponential algorithms and today’s increased processing power, is a practical solution to complex testing challenges.

When applied to the detection of run-time errors, abstract interpretation performs a comprehensive verification of all risky operations and automatically provides a diagnostic of “proven,” “fail,” “unreachable,” or “unproven” for each operation. Engineers can use abstract interpretation to obtain results at compilation time, the earliest stage of the testing.

**Applying Abstract Interpretation**

To better understand how abstract interpretation works, consider a program, $P$, that uses two variables, $X$ and $Y$. It performs the operation:

$$X = X / (X - Y)$$

To check this program for run-time errors, we identify all possible causes for error on the operation:

- $X$ and $Y$ may not be initialized
- $X - Y$ may overflow or underflow
- $X$ and $Y$ may be equal and cause a division by zero
- $X / (X - Y)$ may overflow or underflow

While any of these conditions could cause a run-time error, the following steps focus on the possibility of division by zero.

We can represent all possible values of $X$ and $Y$ in program $P$ on a diagram. The red line in Figure 1 represents the set of $(X, Y)$ values that would lead to a division by zero.

*Figure 1: All possible values of $X$ and $Y$ in program $P$.]*
An obvious way to check for division by zero would be to enumerate each state and determine whether it is on the red line. This is the approach taken by conventional white-box testing, but it has fundamental limitations. First, the number of possible states in a real-world application is typically very large because there are many variables in use. It would take years to enumerate all possible states, making an exhaustive check all but impossible.

In contrast to the brute force approach of enumerating all possible values, abstract interpretation establishes generalized rules to manipulate the whole set of states. It builds an abstraction of the program that can be used to prove properties.

One example of such an abstraction, called type analysis, is shown in Figure 2. This type of abstraction is used by compilers, linkers, and basic static analyzers by applying type inference rules. In type analysis, we project the set of points on the X and Y axes, get the minimum and maximum values for X and Y, and draw the corresponding rectangle. Since the rectangle includes all possible values of X and Y, if a property is proven for the rectangle, it will be valid for the program. In this case, we are interested in the intersection between the red line and the rectangle, because if the intersection is empty, there will never be a division by zero.

![Figure 2. Type analysis projects all values of X and Y onto the axes.](image)

The key drawback of type analysis is that the rectangle includes too many unrealistic values of X and Y. This yields poor, imprecise results and generates a large number of warning messages that often go unread, if the engineer does not switch them off altogether.

Instead of large rectangles, abstract interpretation establishes rules to build more precise shapes, as in Figure 3. It uses techniques based on integer lattices, union of polyhedra, and Groebner bases to represent relationships between data (X and Y) that take into account control structures (such as if-then-else, for and while loops, and switch), inter-procedural operations (function calls), and multitask analysis.

![Figure 3. Abstract interpretation establishes rules to build more precise shapes representing relationships between X and Y.](image)
Unlike compilers and static analyzers, abstract interpretation does not rely solely on the idea of computing relationships between data types and constant values. Instead, it derives these relationships from the semantics of each operation and operand in the program, and uses them as guides to inspect the source code.

With abstract interpretation the following program elements are interpreted in new ways:

- An index in a `for` loop is no longer an integer but a monotonic increasing discrete function from lower to upper limit.
- A parameter passed to a function is no longer a variable or a constant, but a set of values that may be used to constrain the local data used in the function.
- Any global shared data may change at any time in a multitask program, except when protection mechanisms, such as memory locks or critical sections, have been applied.
- A pointer is a data type that may create aliases between explicit data and generate side effects and hidden concurrent accesses on shared data in multitasking applications.
- A variable not only has a type and a range of values, but also a set of equations (including control flow sensitive relationships) that build it.
- Ultimately, run-time errors are equations, also called correctness conditions, that abstract interpretation can solve, using the equations that tie variables together.

Examples of Abstract Interpretation

The following examples are common code constructs that produce run-time errors automatically detected by abstract interpretation.

**Control structure analysis: Out-of-bounds pointer dereferencing after a `for` loop**

```plaintext
10: int ar[100];
11: int *p = ar;
12: int i;
13: for (i = 0; i < 100; i++, p++)
14:   { *p = 0;}
15: *p = 5;
```

In this example, `p` is a pointer that can be abstracted as a discrete increasing function varying by 1 from the beginning of the array `ar`. Upon exiting the `for` loop when `i` equals 100, the pointer `p` is also increased to 100. This cause pointer `p` to be out-of-bounds at line 15, as the array index ranges from 0 to 99. Abstract interpretation would prove this piece of code reliable and would identify line 15 as the source of a run-time error.
Control structure analysis: Out-of-bounds array access within two nested for loops

20: int ar[10];
21: int i,j;
22: for (i = 0; i < 10; i++)
23: {
24:   for (j = 0; j < 10; j++)
25:   {
26:     ar[i - j] = i + j;
27:   }
28: }

Both i and j are variables that are monotonically increasing by 1 from 0 to 9. The operation i–j used as an index for array ar will eventually return a negative value. Abstract interpretation of this code would prove this code reliable and would identify the out-of-bounds array access at line 26.

Note that the run-time errors in these examples often lead to corruption of the data stored near array ar. Depending on how and when this corrupted data is used elsewhere in the program, debugging this kind of error without abstract interpretation can take considerable effort.

Inter-procedural analysis: Division by zero

30: void foo (int* depth)
31: {
32:   float advance;
33:   *depth = *depth + 1;
34:   advance = 1.0/(float)(*depth);
35:   if (*depth < 50)
36:     foo (depth);
37: }
38:
39: void bug_in_recursive ()
40: {
41:   int x;
42:   if (random_int())
43:   {
44:     x = -4;
45:     foo ( &x );
46:   }
47:   else
48:   {
49:     x = 10;
50:     foo ( &x );
51:   }
52: }

In this function, depth is an integer that is first increased by 1. It is then used as a denominator to determine the value of advance and thereafter is recursively passed to the function foo. Checking whether the division
operation at line 34 will cause a division by zero requires an inter-procedural analysis to determine which values will be passed to the function \texttt{foo} (see \texttt{bug_in_recursive}, lines 45 and 50), as it will determine the value of \texttt{depth}.

In the preceding code, the function \texttt{foo} can be called in two different circumstances in the function \texttt{bug_in_recursive}. When the if statement at line 42 is false, \texttt{foo} is called with a value of 10 (line 50).

Therefore, \texttt{*depth} becomes a monotonic discrete increasing function varying by 1 from 11 to 49. The equation at line 34 will not return a division by zero.

However, when the if statement at line 42 is true, then \texttt{foo} is called with a value of -4. Therefore, \texttt{*depth} becomes a monotonic discrete increasing function varying by 1 from -3 to 49. Eventually, \texttt{*depth} will be equal to 0, causing the equation at line 34 to return a division by zero.

A simple syntax check will not detect this error, nor will all test cases. Abstract interpretation will prove all the code reliable except line 45. This illustrates the unique ability of abstract interpretation to perform inter-procedural analysis and distinguish problematic function calls from acceptable ones. If not fixed, a division by zero error will cause processor halt. This kind of error can also require significant debugging time due to the recursive constructs in use.

\textbf{Multitask analysis: Concurrent access to shared data}

Abstract interpretation handles control and data flow analysis and is capable of checking multitasking applications. A key concern with such applications is ensuring that shared data and critical resources have no unexplained concurrent access.

Data aliasing and task interleaving make it difficult to find this type of concurrent access problem.

With data aliasing, pointers are used for shared memory access. This approach can create hidden or implicit relationships between variables, so that one variable may be unexpectedly modified during program execution through pointers, causing sporadic anomalies. The analysis of this problem requires very efficient pointer analysis algorithms. With abstract interpretation these can be implemented to provide a list of shared data and the list of read and write accesses by functions and tasks along with the related concurrent access graph.

Tasks interleaving makes multitask applications problematic to debug because bugs are very difficult to reproduce when they depend on a sequence of tasks being executed in a specific order in real-time. Abstract interpretation takes every possible interleaving of tasks into account, for a complete control flow analysis. Constructing these results or the concurrent access graph by hand would be exceptionally difficult.

\textbf{Benefits of Abstract Interpretation for Run-time Error Detection}

Abstract interpretation is an efficient, cost-effective, and rapid way to ensure delivery of reliable embedded systems. It provides four benefits: assurance of code reliability, increased efficiency, reduced overhead, and simplified debugging.

\textbf{Assurance of code reliability}

Through its exhaustive code review, abstract interpretation not only enables run-time error detection, but also proves code correctness. This is especially important in safety-critical applications in which system failures can be catastrophic. Traditional debugging tools are tuned to detect errors but do not verify the reliability of the
remaining code. Abstract interpretation makes it possible to identify code that will never cause a software fault, thereby removing any uncertainty about the software’s reliability.

**Increased efficiency**
By verifying the dynamics of applications, abstract interpretation lets embedded developers and testers identify the code sections in their program that are free of run-time errors from the ones that will lead to a reliability breach. Because errors can be identified before code is compiled, abstract interpretation helps teams realize substantial time and cost savings by finding and eliminating run-time errors when they are easiest to fix.

**Reduced overhead**
Abstract interpretation requires no execution of the software, so it produces thorough results without the overhead of writing and executing test cases. Likewise there is no need to instrument code and then strip out the instrumentation before shipping software. In addition, abstract interpretation can be implemented in ongoing projects without changing existing development processes.

**Simplified debugging**
Abstract interpretation streamlines debugging because it directly identifies the source of each error, not just its symptom. It eliminates time wasted tracking crashes and data corruption errors back to their source, as well as the time previously spent trying to reproduce sporadic bugs. Abstract interpretation is repeatable and exhaustive. Each operation in the code is automatically identified, analyzed, and checked against all possible combinations of input values.

**Run-Time Errors Detected by Abstract Interpretation**
- Concurrent accesses to shared data
- Pointer de-referencing issues (null, out-of-bounds accesses)
- Out-of-bounds array accesses
- Read accesses to non-initialized data
- Invalid arithmetic operations (such as division by zero, and square root of negative numbers)
- Float, integer overflow/underflow
- Illegal type conversion (for example, float J int, long J short)

**Other Dynamic Properties Detected by Abstract Interpretation**
- Unreachable code
- Non-termination of loops
- Initialized return values

**Abstract Interpretation Tools**
The following products from The MathWorks are the only commercially available code verification tools that implement abstract interpretation:
- PolySpace™ Client for C++
- PolySpace™ Server for C/C++
- PolySpace™ Client for Ada
- PolySpace™ Server for Ada

For more information, visit [www.mathworks.com/polyspace](http://www.mathworks.com/polyspace)